

QUANTUM COMPUTING WITH TRAPPED IONS



JOHANNES GUTENBERG
UNIVERSITÄT MAINZ

www.quantenbit.de

Ferdinand Schmidt-Kaler
QUANTUM, Univ. Mainz & Helmholtz Inst. Mainz



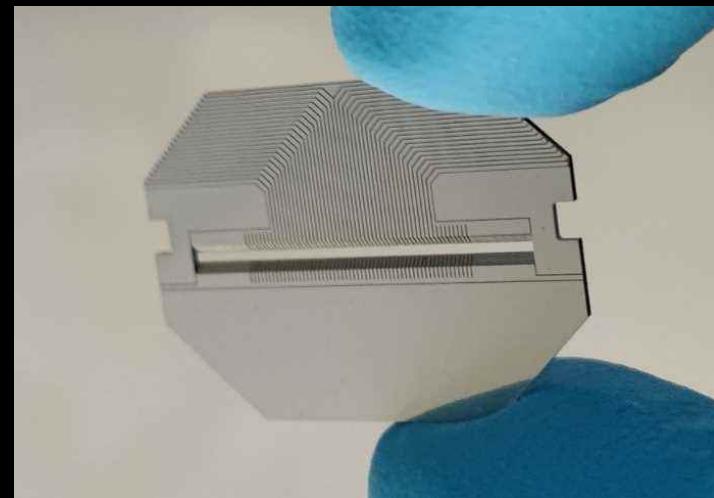
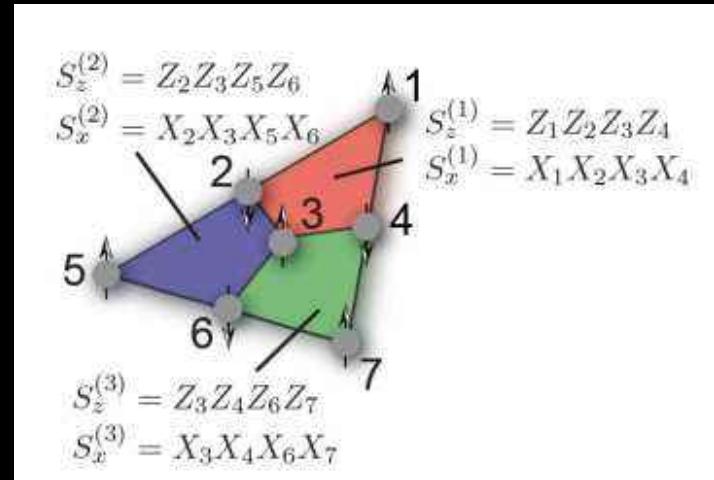
Bundesministerium
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|AT|Q>



Menue

- Trapped ion qubit introduction
- Fault-tolerant parity readout
for quantum error correction
- Scaling up trapped ion QC technology
Hardware & Software
- Application cases for QC
- Fast entanglement generation - Rydbergs



First two-qubit gate proposal

74, NUMBER 20 4091 PHYSICAL REVIEW LETTERS

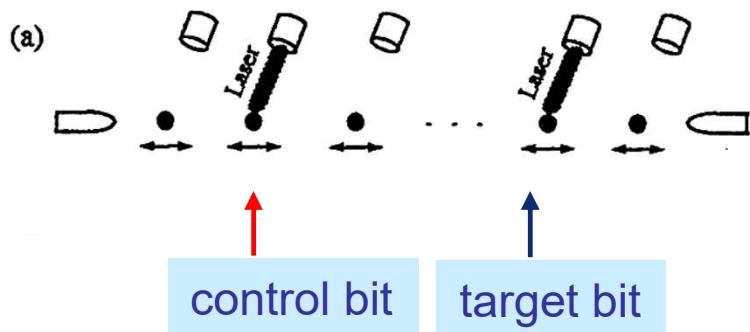
15 MAY 1995

Quantum Computations with Cold Trapped Ions

J. I. Cirac and P. Zoller*

*Institut für Theoretische Physik, Universität Innsbruck, Technikerstrasse 25, A-6020 Innsbruck, Austria
(Received 30 November 1994)*

A quantum computer can be implemented with cold ions confined in a linear trap and interacting with laser beams. Quantum gates involving any pair, triplet, or subset of ions can be realized by coupling the ions through the collective quantized motion. In this system decoherence is negligible, and the measurement (readout of the quantum register) can be carried out with a high efficiency.



Cirac, Zoller
PRL74, 4091 (1995)
Schmidt-Kaler et al.,
Nat. 422, 408 (2003)

- single bit rotations and quantum gates
- small decoherence
- unity detection efficiency
- scalable ...

All-to-all qubit coupling is mediated by laser light interactions and com. vibrational modes

two-qubit gate variations

- Cirac Zoller gate
- M\"{o}lmer S\"{o}rensen gate
- Spin-dependent light forces
- Spin-dependent magnetic gradient forces
- Cavity-induced interactions
- Rydberg excitation & blockade interaction
- Rydberg ultra-fast electric kick
- Atom-ion interactions

Cirac, Zoller, PRL 74, 4091 (1995)

Schmidt-Kaler et al., Nat. 422, 408 (2003)

S\"{o}rensen, M\"{o}lmer, PRL 82, 1971
(1999), PRA 62, 022311 (2000)

Leibfried et al., Nature 412, 422 (2003)

Khromova et al, PRL 108, 220502 (2012),
Warring et al, Phys. Rev. A 87, 013437 (2013)

Duan, Kimble, PRL 90, 253601 (2003)

Casabone et al, PRL 111, 100505 (2013)

Takahashi, et al, PRL 124, 013602 (2020)
Krutyanskiy, et al, PRL 130, 050803 (2023)

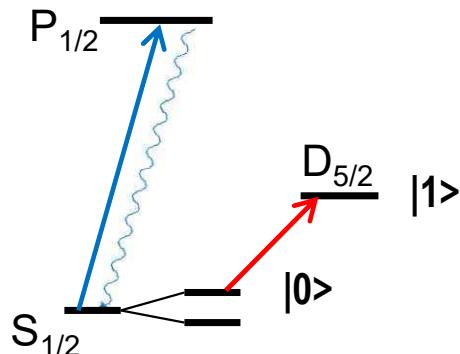
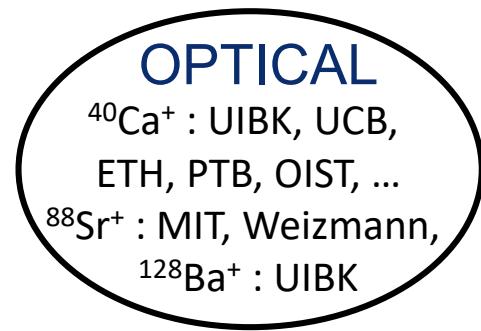
Li, Lesanowsky, Appl. Phys. B 114, 37 (2014)

Zhang, et al, Nat. 580, 345 (2020)

Vogel, et al, PRL 123, 153603 (2019)

Sencker, et al, PRA 94, 013420 (2016)

Choice of ion qubit

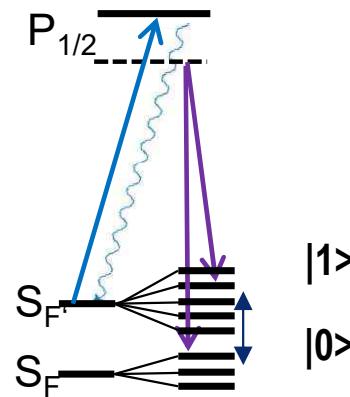


HYPERFINE

$^9\text{Be}^+$: NIST, ETH
 $^{25}\text{Mg}^+$: NIST, Freiburg
 $^{43}\text{Ca}^+$: UIBK, Oxford
 $^{171}\text{Yb}^+$: JQI, Sussex, Duke, ...
 $^{133}\text{Ba}^+$: UCLA...

MICROWAVE

NIST, Siegen, Hannover, Oxford, Sussex, ...

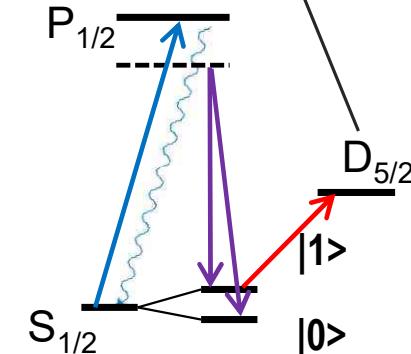


Rydberg

Mainz, Stockholm

SPIN

$^{40}\text{Ca}^+$: Oxford, Mainz, ...



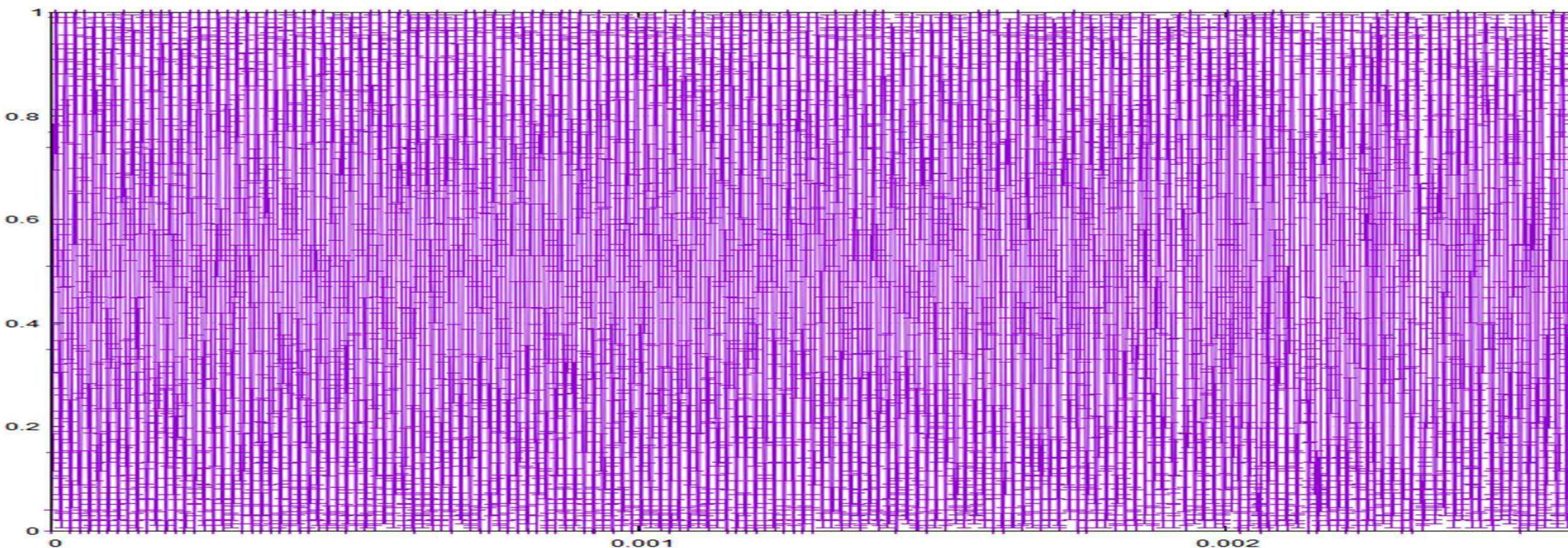
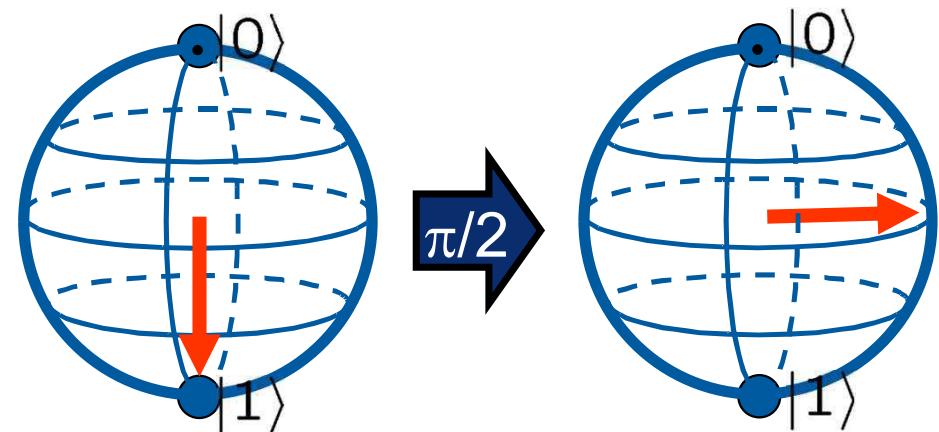
Easy readout
Requires optical phase stability
Limited by metastable lifetime

Infinite T_1
only scattering errors
complicated level scheme

Infinite T_1
only scattering errors
readout overhead

Rotation of an ion qubit

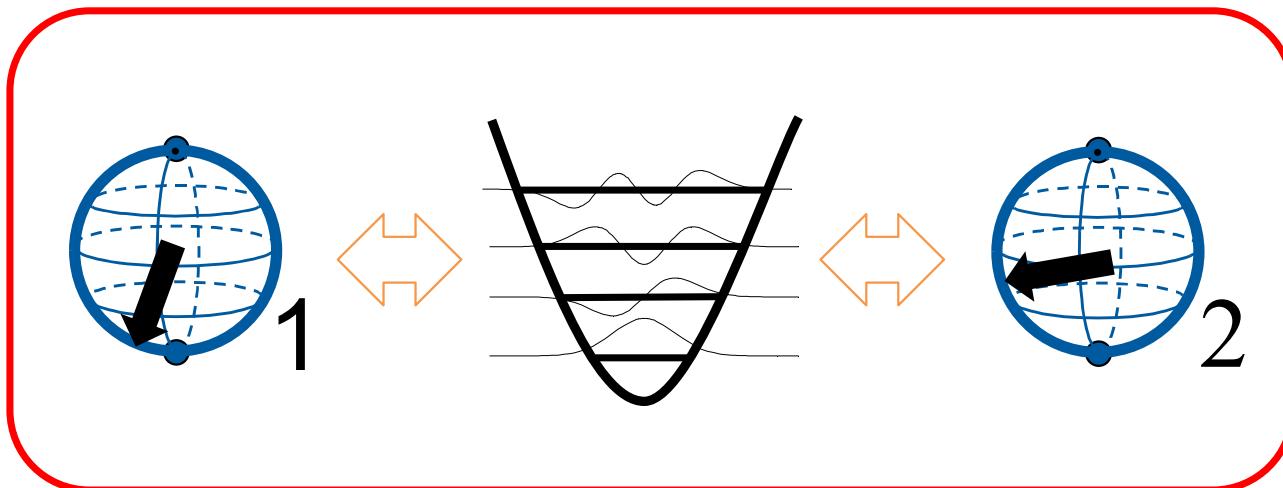
- Driven by laser beams
- >99,99% fidelity gates
- Gate time few μs



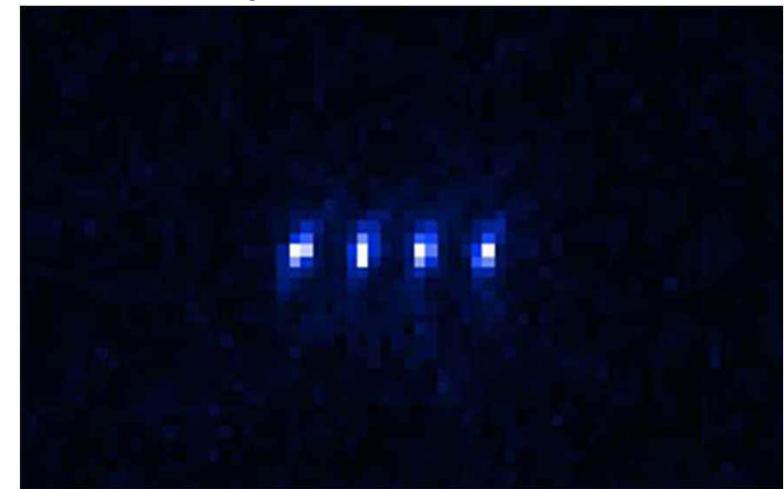
Key figures in trapped ion QC

long-range Coulomb interaction:

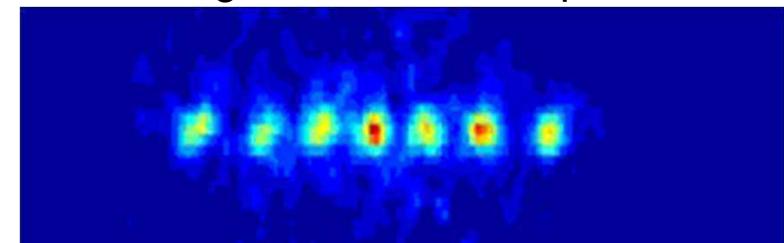
- All-to-all connectivity
- Single shot read-out of spin state better than $1 - 10^{-4}$
- Single gate fidelity better than $1 - 10^{-4} \dots 10^{-5}$
- Two qubit gate fidelity $1 - 10^{-3} \dots 10^{-4}$
- Two-qubit gate operation times $\sim 30 \dots 100 \mu\text{s}$



Quantum jumps



Breathing mode stroboscopic detection



Qubit coupling is mediated by laser light interactions to one or many modes

Spin dependent light force gate

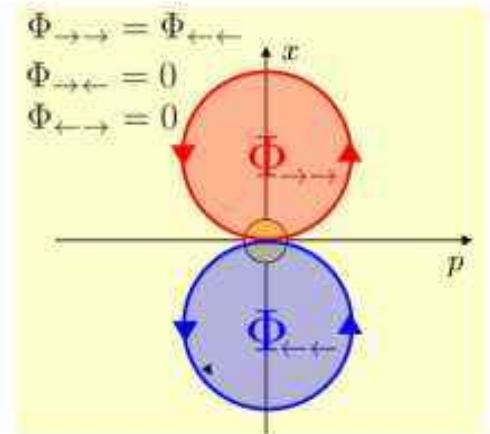
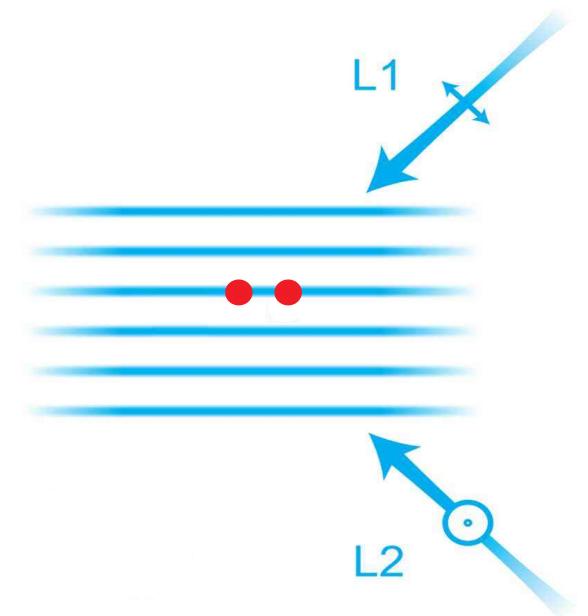
- Lin perp lin lattice generates oscillatory optical dipole force (ODF)
- Near resonant, spin-dependent excitation of gate mediating mode

$$\begin{aligned}\hat{U}(t) &= \lim_{n \rightarrow \infty} \prod_{k=1}^n \exp \left(-\frac{i}{\hbar} \hat{H}_{\text{int}}(t_k) \Delta t \right) \quad \text{with } \Delta t = t/n, t_k = k \Delta t \\ &= \lim_{n \rightarrow \infty} \prod_{k=1}^n \hat{D} (\Omega e^{i \delta t_k} \Delta t) \\ &= \hat{D}(\alpha(t)) e^{i \Phi(t)} \quad \text{with} \quad \hat{D}(\alpha(t)) = e^{\alpha(t) \hat{a}^\dagger - \alpha^*(t) \hat{a}},\end{aligned}$$

$$\hat{H}_{\text{int}}(t) = \hbar \Omega i (\hat{a}^\dagger e^{i \delta t} - \hat{a} e^{-i \delta t}) (\hat{\sigma}_z \otimes \mathbb{1} + \mathbb{1} \otimes \hat{\sigma}_z) \quad \text{for two ions and one mode}$$

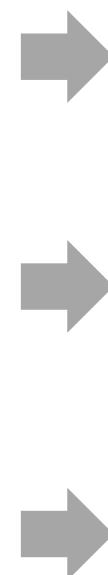
$\alpha(t) = i \frac{\Omega}{\delta} (1 - e^{i \delta t})$	displacement	δ detuning
$\Phi(t) = \left(\frac{\Omega}{\delta} \right)^2 (\delta t - \sin(\delta t))$	phase	Ω Amplitude $2\pi/\delta$ return time

$$\begin{aligned}\{|00\rangle, |11\rangle\} &\rightarrow e^{i\Phi} \{|00\rangle, |11\rangle\} \\ \{|01\rangle, |10\rangle\} &\rightarrow \{|01\rangle, |10\rangle\}.\end{aligned}$$



Scalable quantum computing architectures

- ❑ Number of qubits
- ❑ Qubit-connectivity
- ❑ Fidelity of gate operations
- ❑ Qubit preparation & readout fidelity
- ❑ In-loop qubit readout
- ❑ Real-time feedback on quantum algorithm
- ❑ Low latency connection to
high performance computer



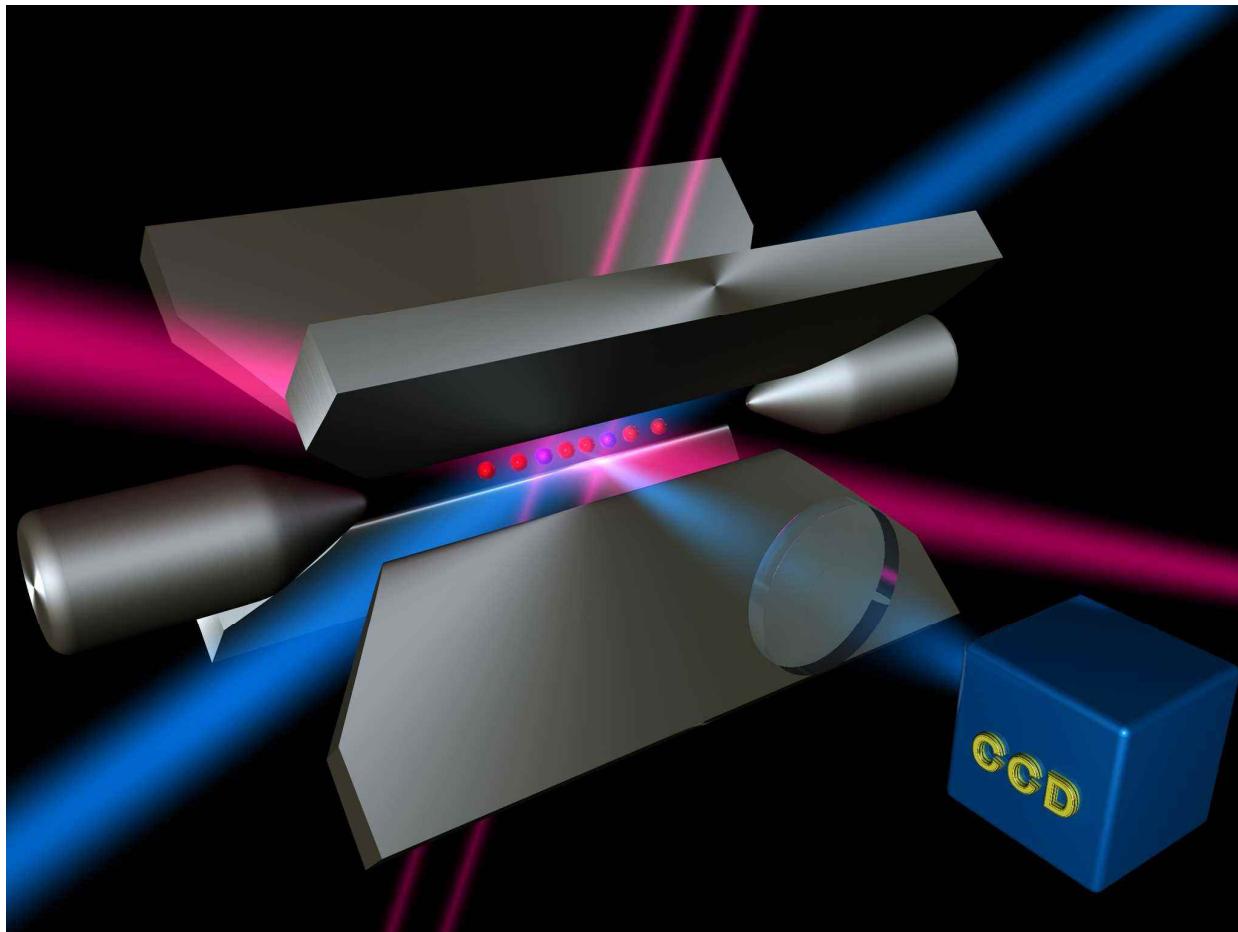
Quantum-volume

Quantum
error correction

Hybrid
computing

Linear crystal processor

Static trapped ion registers >20 qubits



- Long linear crystals
- Individual single ion addressing for gates

Nägerl, et al, PRA 60, 145 (1999)
Friis, et al, Phys Rev X. 8 021012 (2018)
Korenblit et al, NJP 14, 095024 (2012)
Egan et al., Nat. 598, 281 (2021)

Quantum-CCD architecture

- Laser pulses generate entanglement
- Segmented micro trap allows controlling the ion positions

DIVIDE ET IMPERA

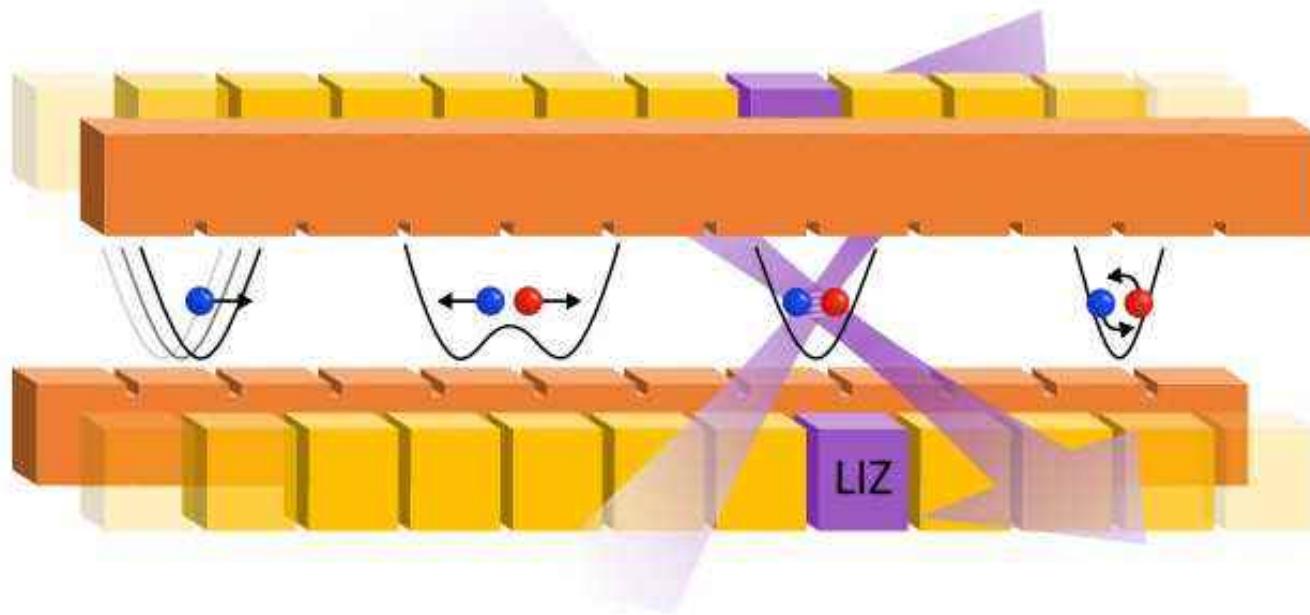
Dave Wineland – vision of scalable QC
using shuttles in segmented ion traps

Kielpinski et al., Nat.
417, 709 (2002)

Honeywell Quantum
Solutions

Our quantum computing future is built on our
technology heritage.

Ion movement – qubit register reconfiguration



- Shuttle single ion
- Shuttle ion crystal
- Separate two-ion crystal
- Merge into two-ion crystal
- Swap ion positions

Geometric phase gate
with 99.85% fidelity
on **radial** mode

Single qubit rotation with
average EPG of $7.8 \cdot 10^{-5}$

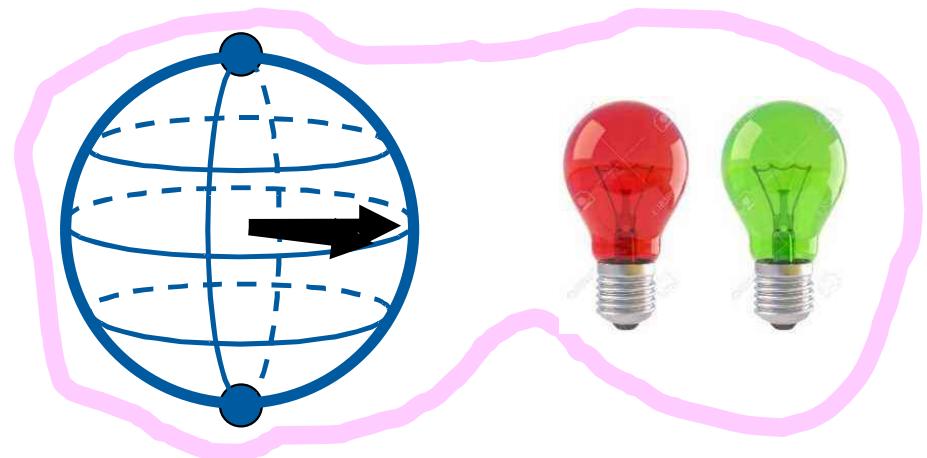
Kielpinski et al., Nat. 417, 709 (2002)
Walter et al., PRL109, 080501 (2012)
Kaufmann et al, NJP 16, 073012 (2014)
Kaufmann et al, RPA 95, 052319 (2017)
Kaufmann et al, PRL 119, 150503 (2017)
Kaustal et al, Adv. At. Mol. Opt. Phys. 69, 233 (2020)

How to digitize analog quantum errors ?

qubit $|\Psi\rangle = \alpha|0\rangle + \beta|1\rangle$

entangle qubit with ancilla

$$|\Psi\rangle_{\text{no error}} |A\rangle_{\text{no error}} \oplus |\Psi\rangle_{\text{full error}} |A\rangle_{\text{error}}$$



measure ancilla, and get either...

$$|\Psi\rangle_{\text{no error}} |A\rangle_{\text{no error}} \oplus |\Psi\rangle_{\text{full error}} |A\rangle_{\text{error}}$$

... or

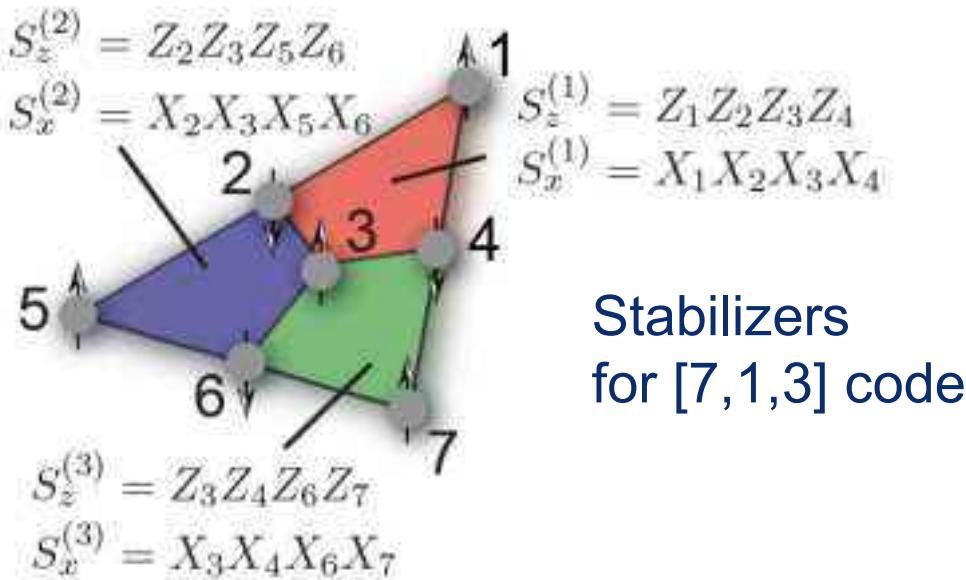
$$|\Psi\rangle_{\text{no error}} |A\rangle_{\text{no error}} \oplus |\Psi\rangle_{\text{full error}} |A\rangle_{\text{error}}$$



Topological QEC

Quantum
eQual

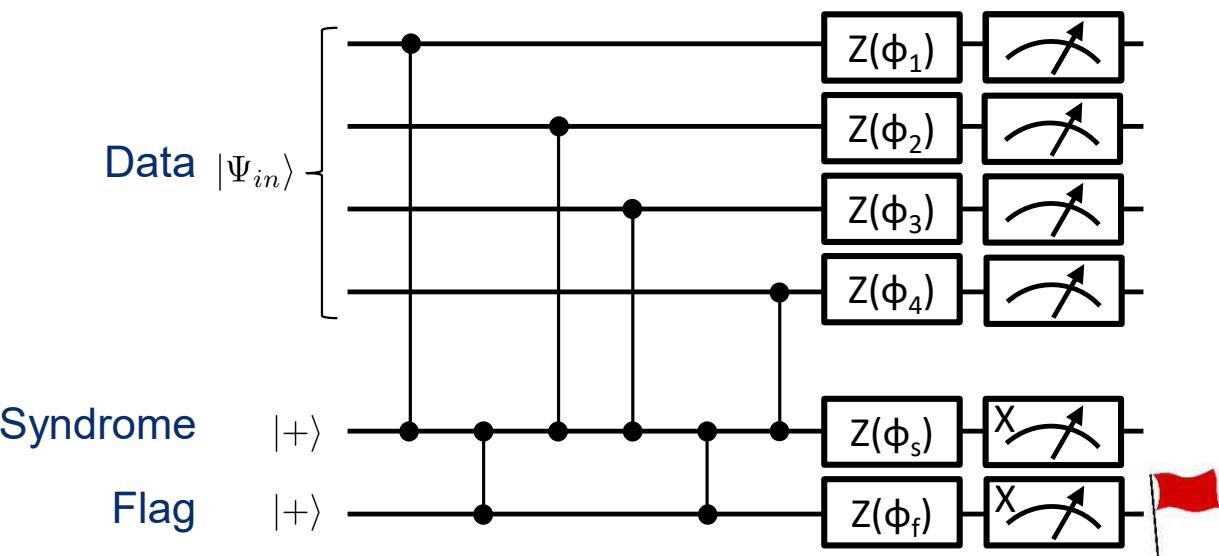
Bermudez et al, Phys. Rev. X 7, 041061
Nigg et al., Sci. 234, 302 (2014)



Logical qubit using
7-data qubit color code

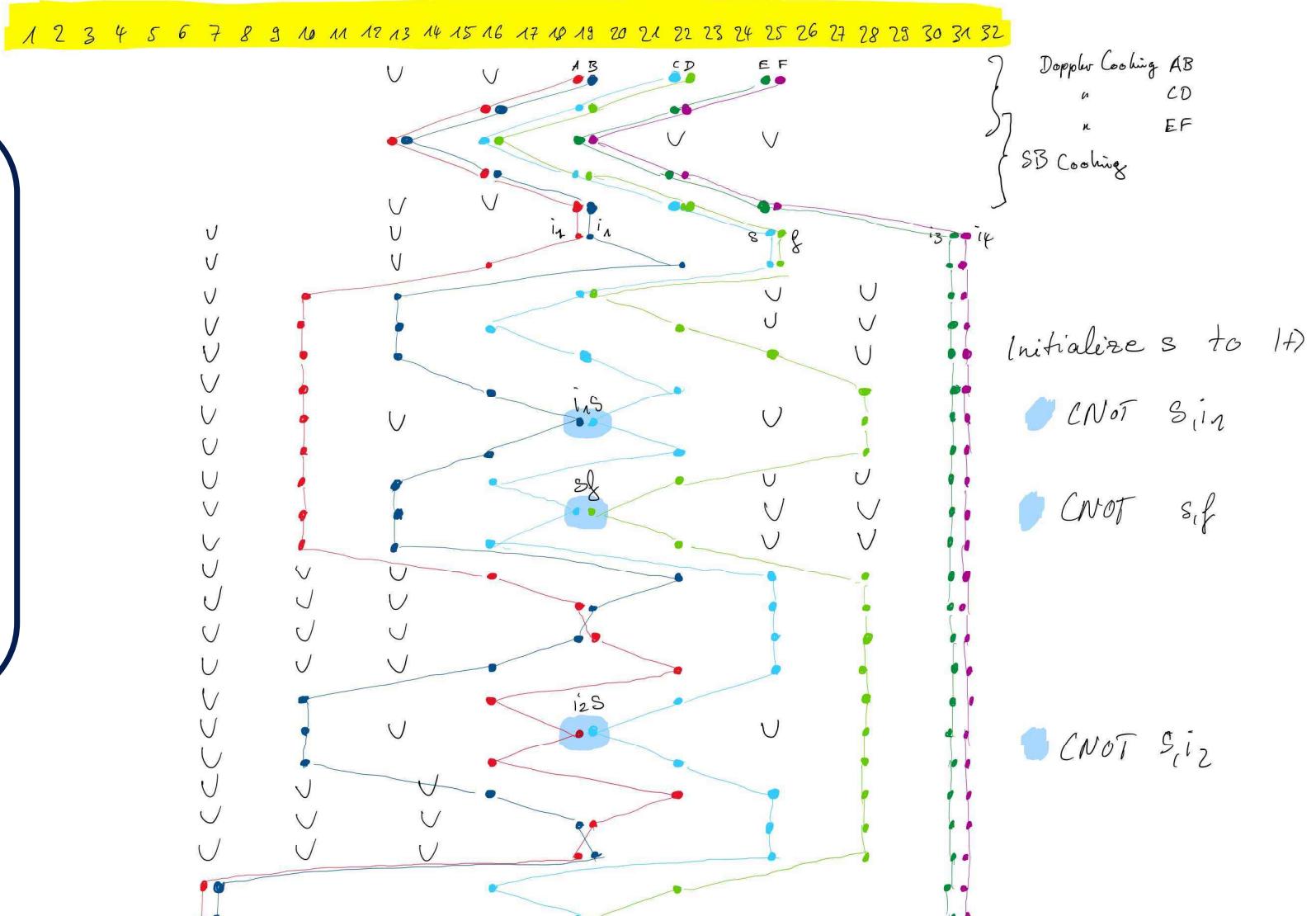
Bermudez et al, arXiv: 1810.09199
Chao, Reichardt, arXiv:1705.02329
Yoder, Kim, Quantum 1, 2 (2017)

Fault-tolerant syndrome
readout of one plaquette

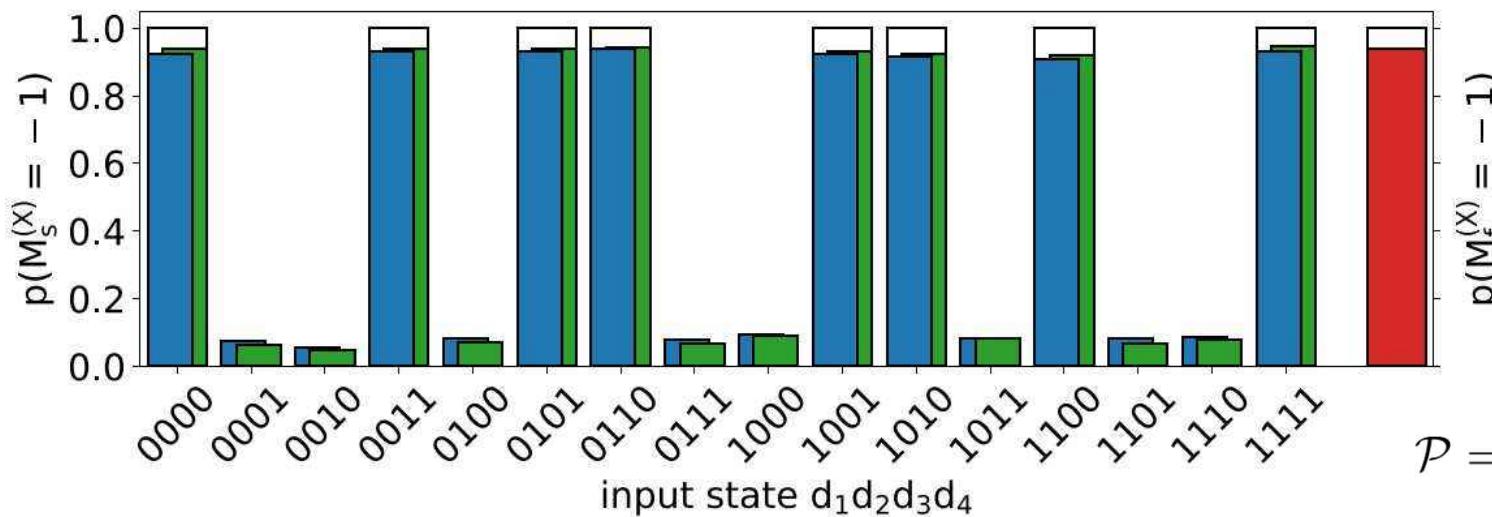


Fault-tolerant syndrome readout

6 ions:
90 configurations
41 two-ion transp.
158 single ion transp.
6 two-ion rotation
21 merge/separate
6 two-qubit gates
6 RAP pulses
6 fluo. det.



Fault-tolerant syndrome readout



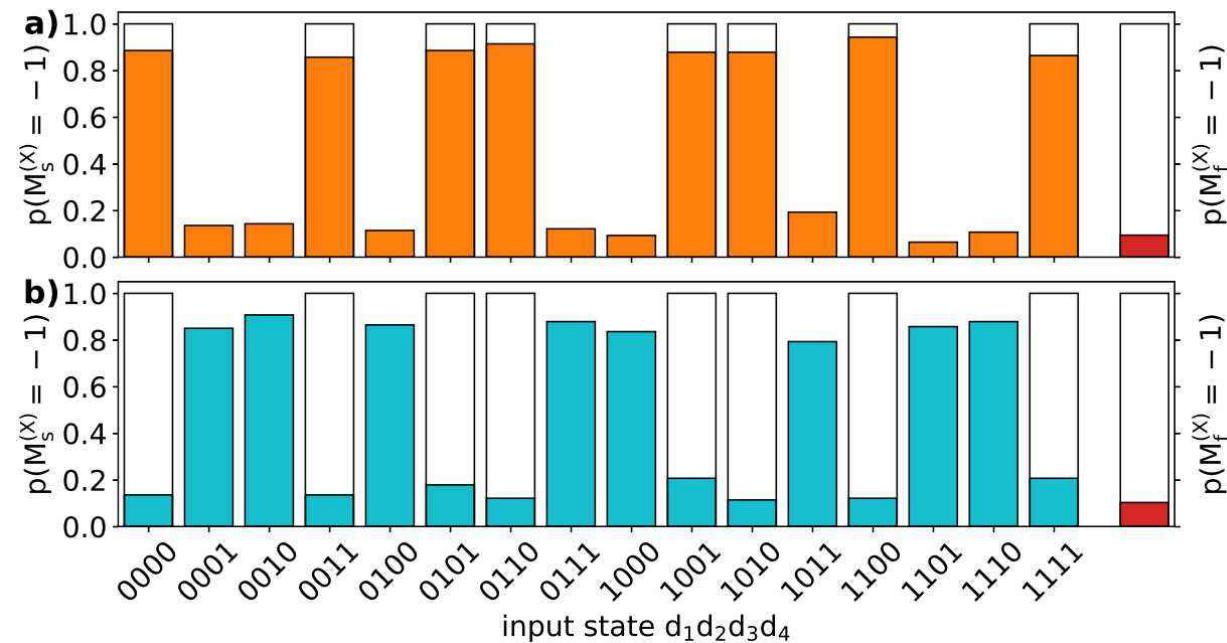
Parity readout fidelity:

$$\mathcal{P} = \frac{1}{2} [p(M_s^{(X)} = -1 \mid P_{in} = +1) + p(M_s^{(X)} = +1 \mid P_{in} = -1)]$$

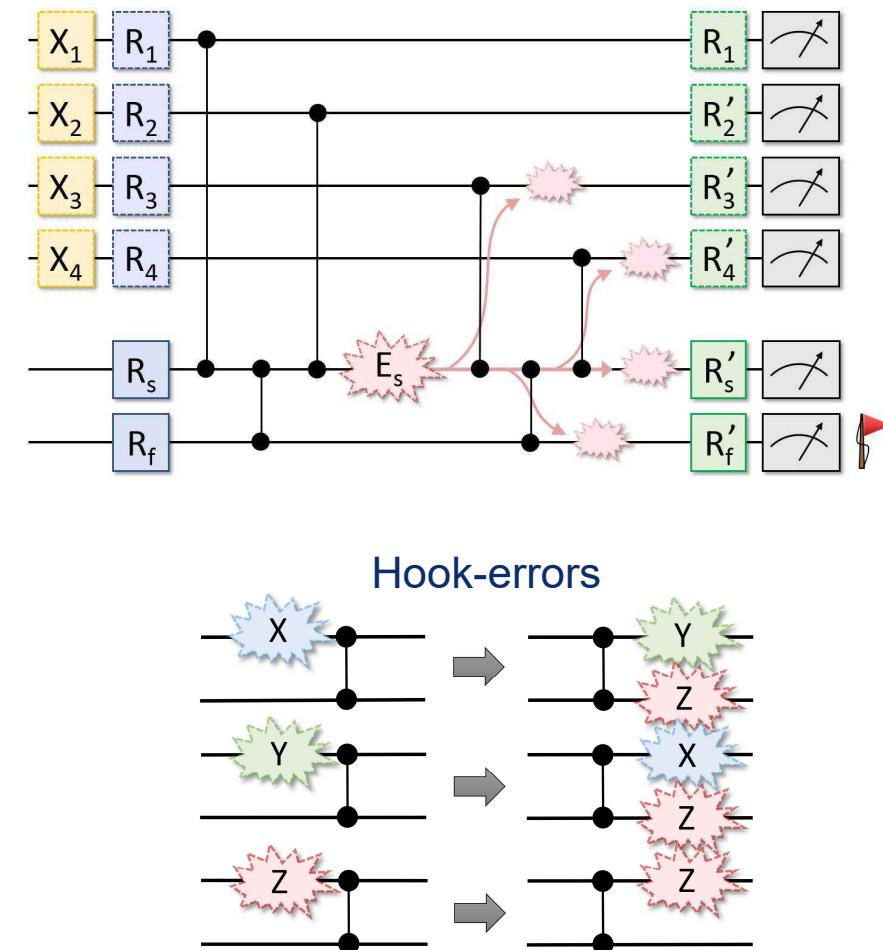
- Single shot fidelity $P=92.3(2)\%$ [blue]
- Flag raised $6.3(2)\%$
- Post-selection on “flag not raised” [green]
 $P=93.2(2)\%$
- Improvement by 4.5σ

Egan et al., Nat. 598, 281 (2021),
 Postler et al, Nature 605, 675 (2022),
 Ryan-A. et al, Phys. Rev. X 11, 041058
 (2021), Debroy et al, Phys. Rev. Lett.
 127, 240501 (2021),
 Ryan-A. et al, arXiv:2208.01863

Error injection

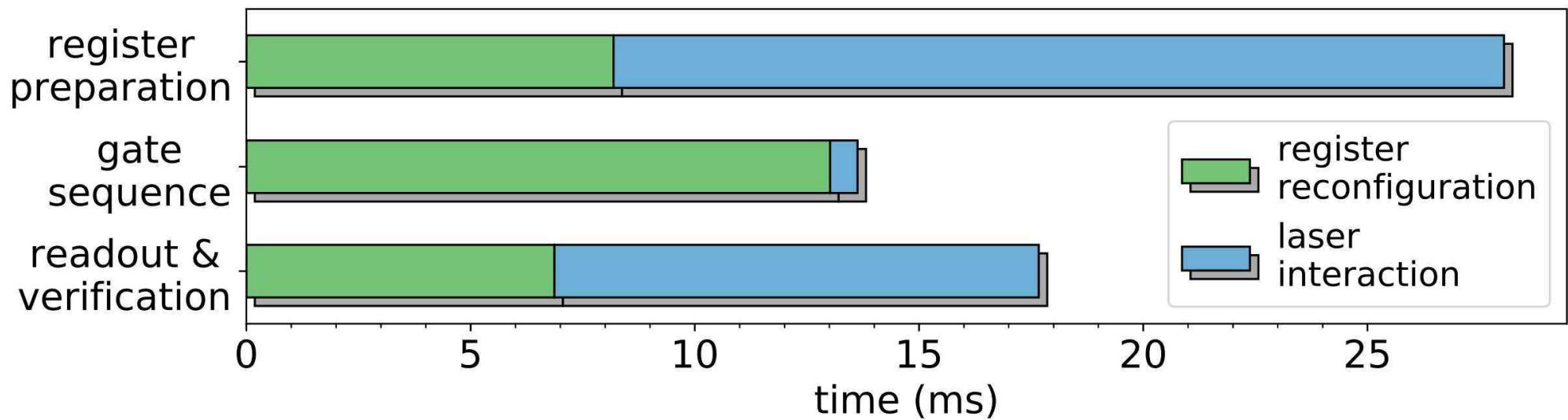


- Insert X or Y error on syndrome
- 90.6(6)% or 88.3(7)% error detection rate



Ryan-A. et al, arXiv 2107.07505
Debroy et al, arXiv 2105.05068

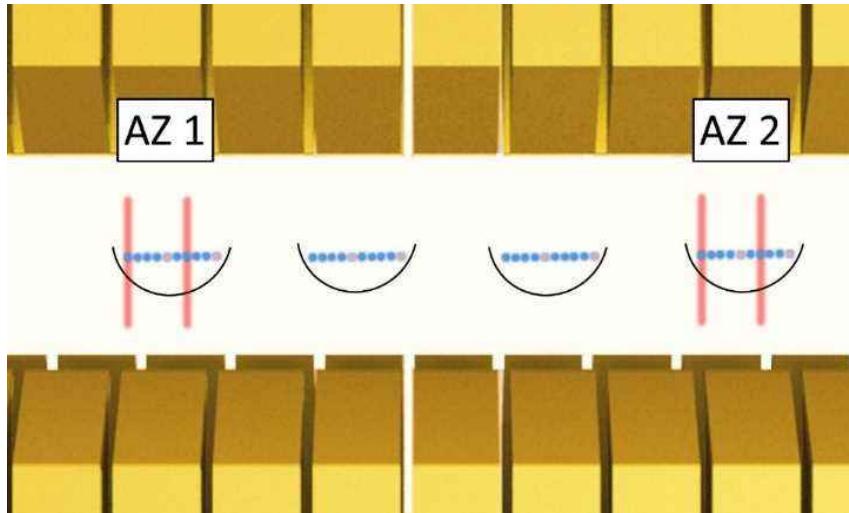
Time budget



- 10% of time used for quantum algorithm

Lesson learned: Save time and be faster!

IQuAn - Architecture



- Multiple zones for individual optical addressing for gates *combined with*
- Reconfiguration of registers, 50 ...100
- Parallel execution of gates and reconfiguration

- Scalable, industry standard optical and electrical control units
- HPC connection
- Funding started 2021



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Levels of connectivity for scalable architecture

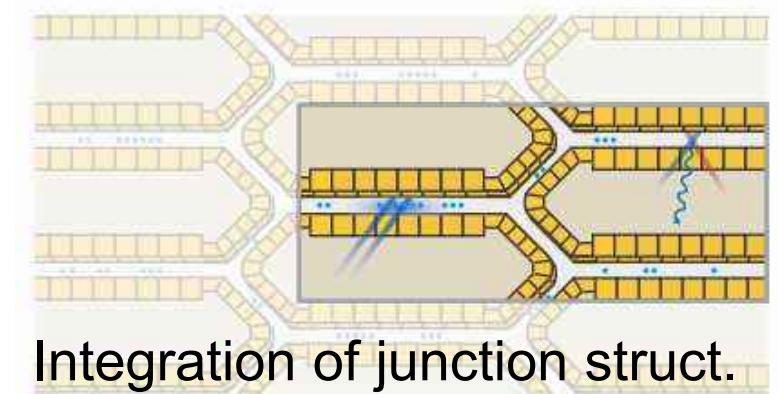
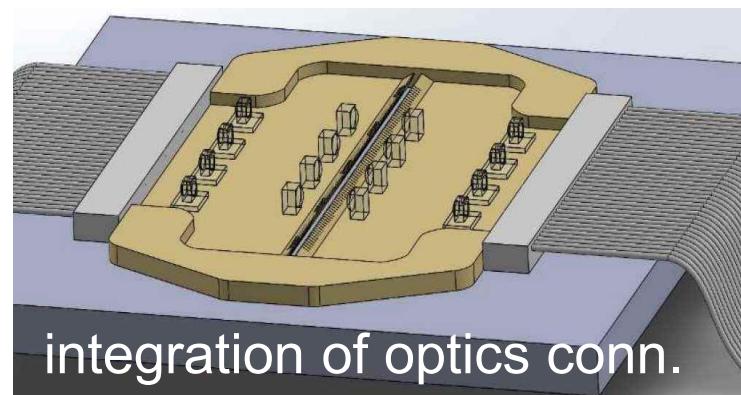


- Level zero: ion qubits couple via common vibration, optical addressing ions
- Level one: combine this with transports of ions in segmented traps, operating multiple optical addressing zones
- Level two: combine this with optical interconnects via high N.A. or fibre optics, alternatively, junctions, ion shuttles in between different trap regions

Stopp, et al, Qu. Sci. Techn. 7 034002 (2022)

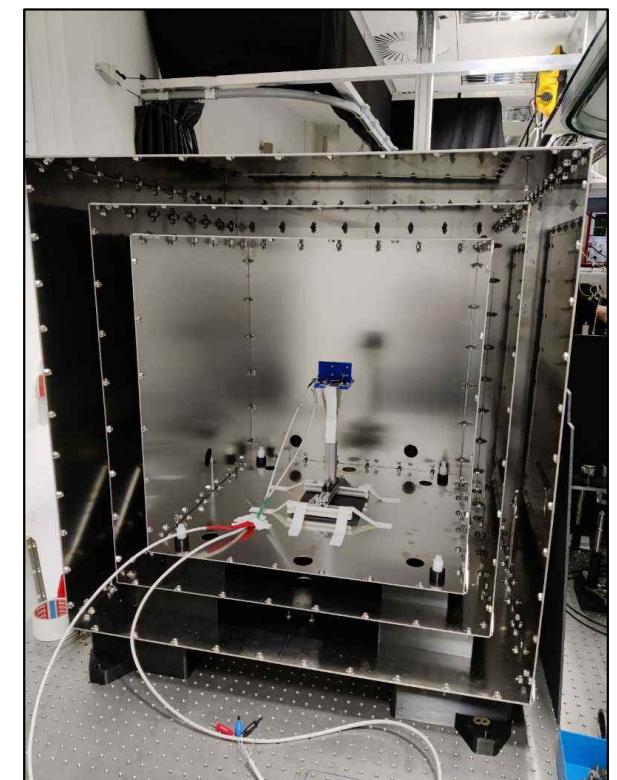
Takahashi, et al, PRL 124, 013602 (2020)

Krutyanskiy, et al, PRL 130, 050803 (2023)



Hardware components & control modules

- SLE Ion traps / 40 segments
- High optical access Ti-UHV vessel
- 3-layer μ-metal shield
- Laser racks, fiber coupled
- Light processing units
- DC and RF multichannel AWGs

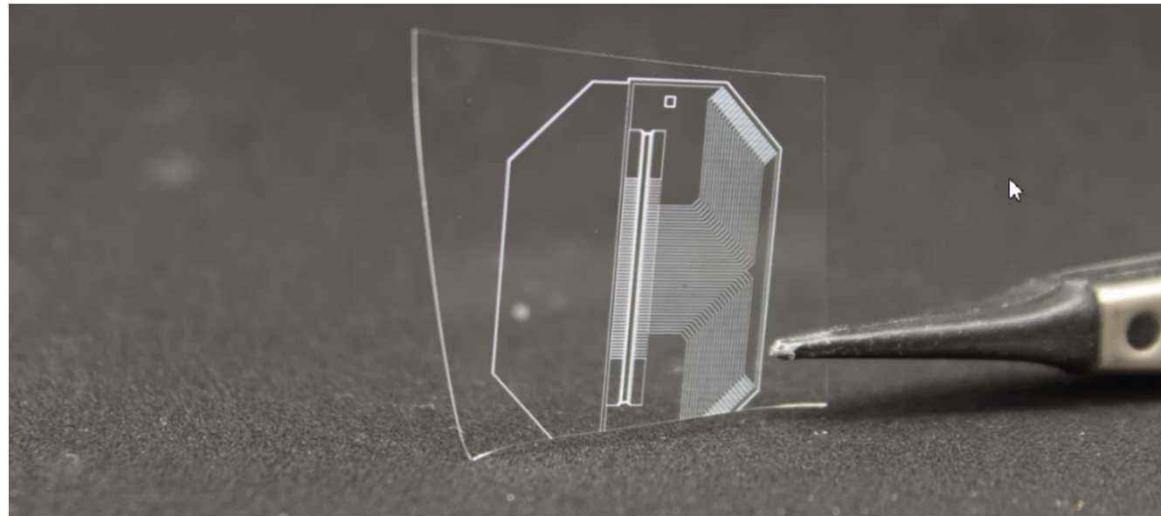


TRAPS cleanroom

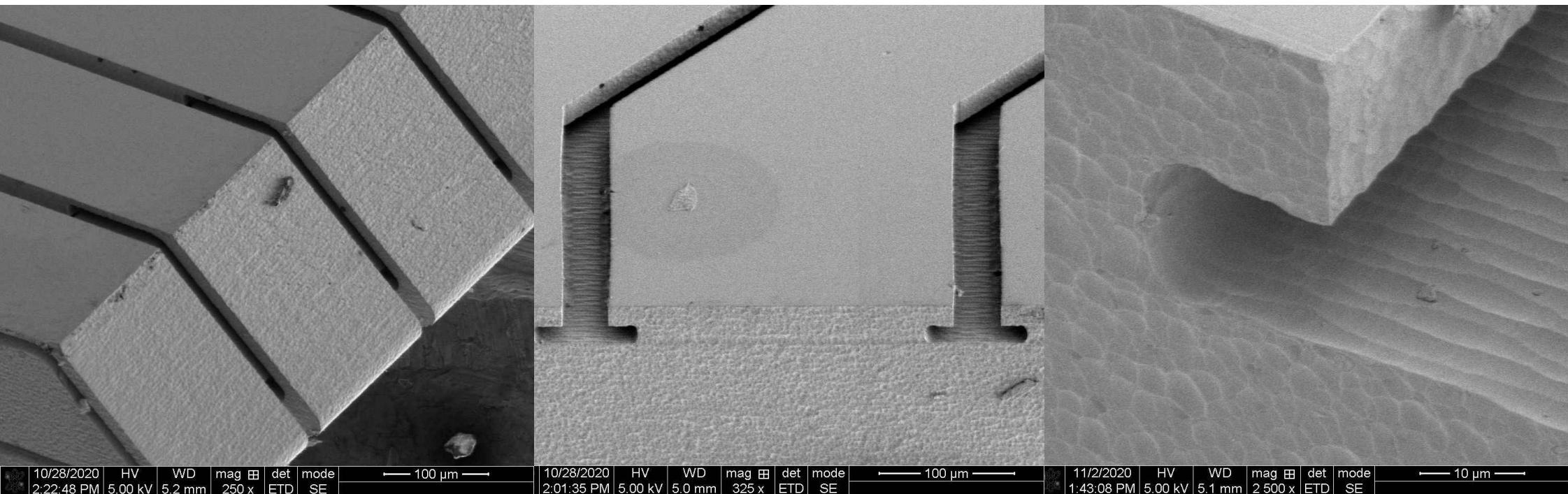
- SLE trap fab.
- Sputter, dicer, asher
- Wet bench,
- Microscopes, wire bonder



SLE written structures



See also: Ragg et al, Rev. Sci. Instr. 90, 103203 (2019)



10/28/2020	HV	WD	mag	det	mode	— 100 μm —	10/28/2020	HV	WD	mag	det	mode	— 100 μm —	11/2/2020	HV	WD	mag	det	mode	— 10 μm —
2:22:48 PM	5.00 kV	5.2 mm	250 x	ETD	SE		2:01:35 PM	5.00 kV	5.0 mm	325 x	ETD	SE		1:43:08 PM	5.00 kV	5.1 mm	2 500 x	ETD	SE	

**Reliable optical qubit control,
get free space in the lab**

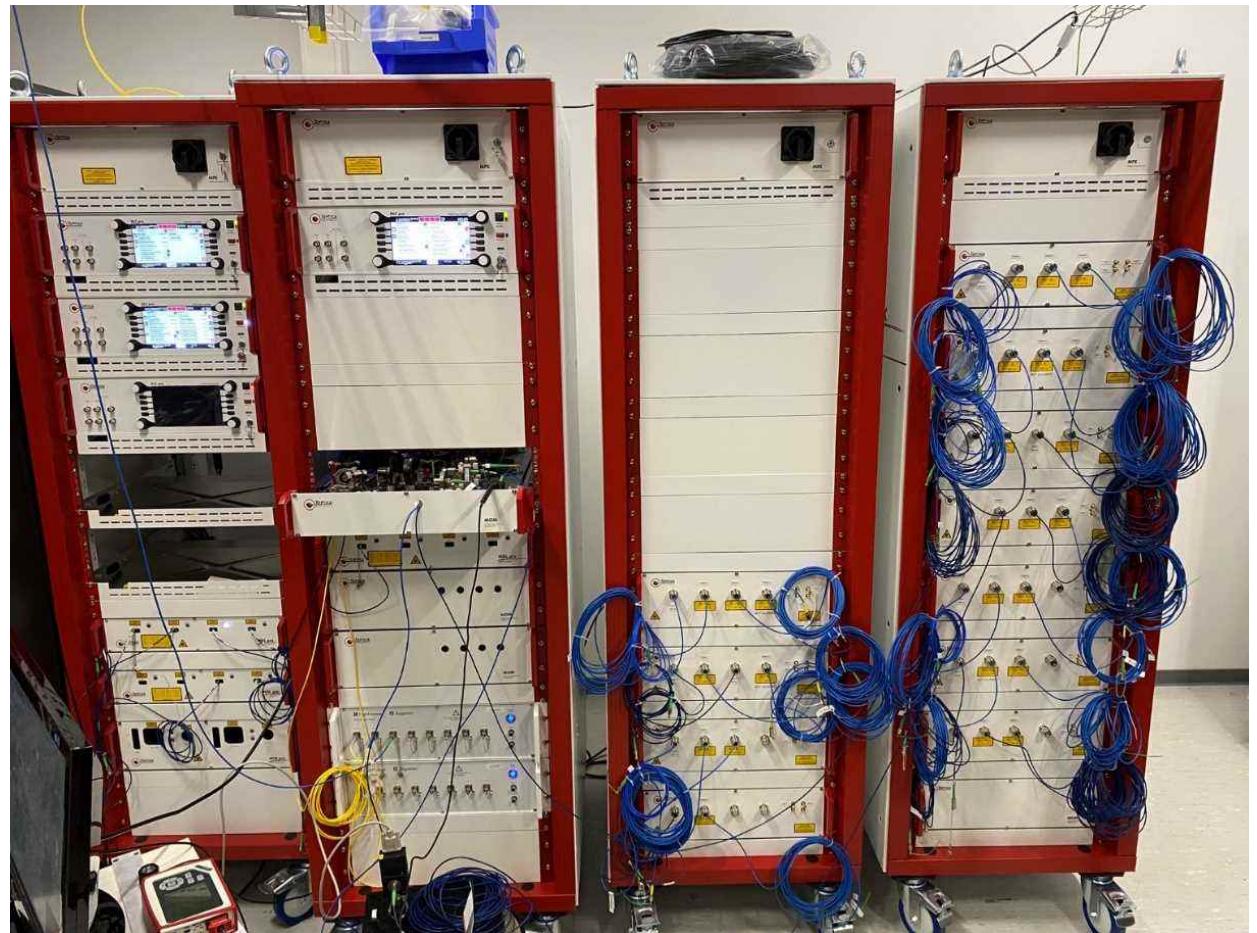
IQuAn

|ATI|Q+



Rackmount laser units

- Laser sets for $^{40/44}\text{Ca}$
Sympathetic cooling of
radial modes
- LPUs: (rack-based light
processing units)
 - for switching of light
 - FM-EOMs
 - automatic fiber coupling
 - outstanding stability
- Frequency locking by
wavemeter and ultra stable
cavities (rack-based)

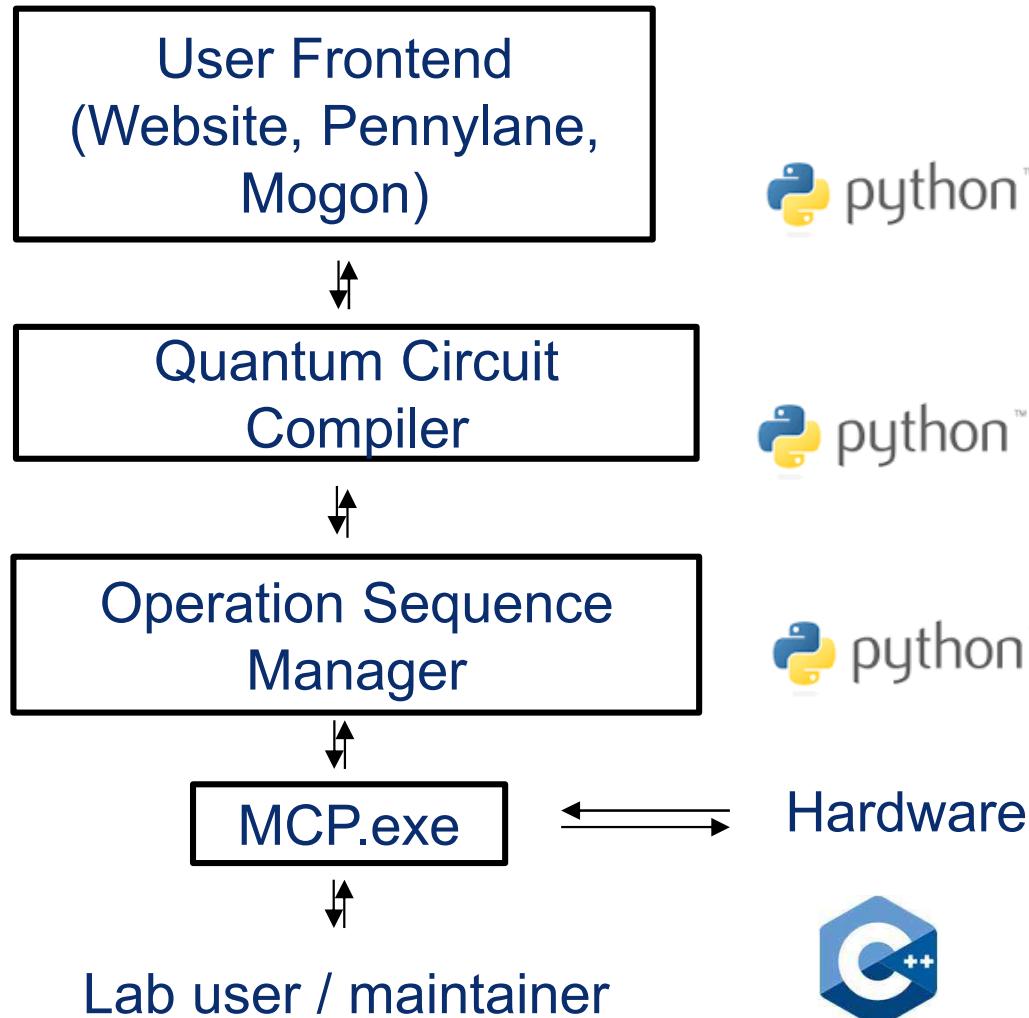


Quantum computer control room





Software stack



User interaction via

- Drag & Drop Circuit Builder
- OpenQASM
- Pennylane & Qiskit
- HPC Mogon II connection
- Integration of user management and database



Quantum circuit optimizer

- Converts quantum circuit into native gate set
 - Optimizes the quantum circuit with respect to shuttling overhead and number of gates
 - SWAP elimination
 - Different degrees of optimization possible
 - Macro-matching & phase tracking
 - Gate count reduction by 3.6 (as compared to Pytket)
 - Similar performance as AQT compiler, but for shuttle-based situation
- $$\mathcal{M} = \{\text{R}(\theta, \phi), \text{Rz}(\phi), \text{ZZ}(\theta)\}$$

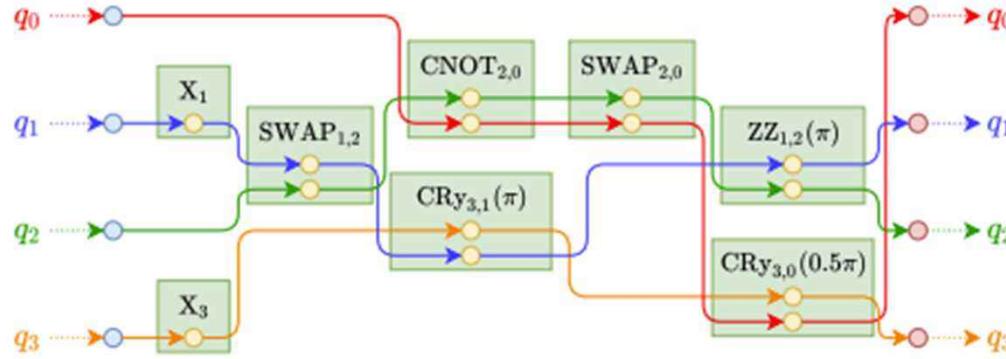
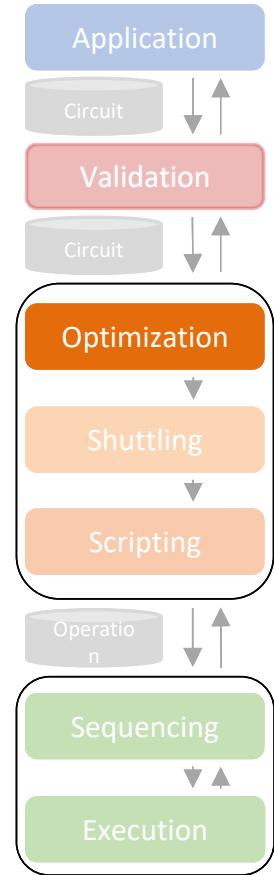
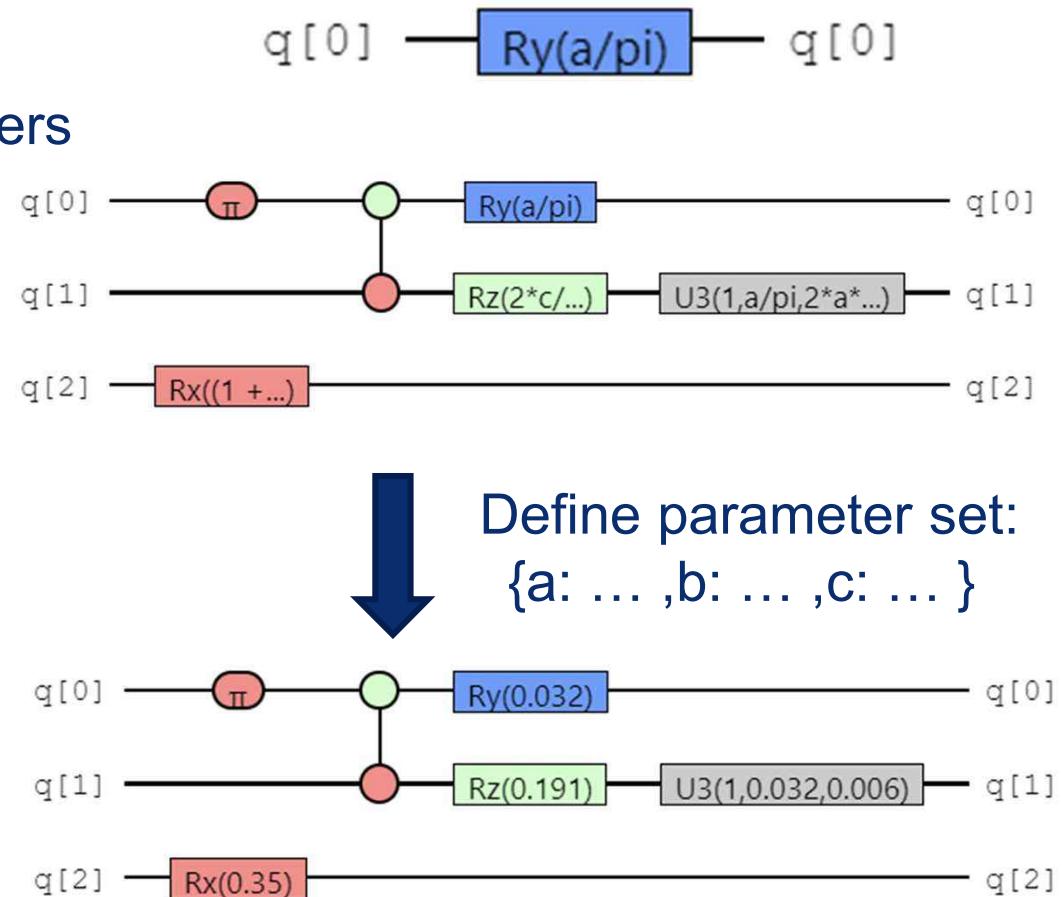
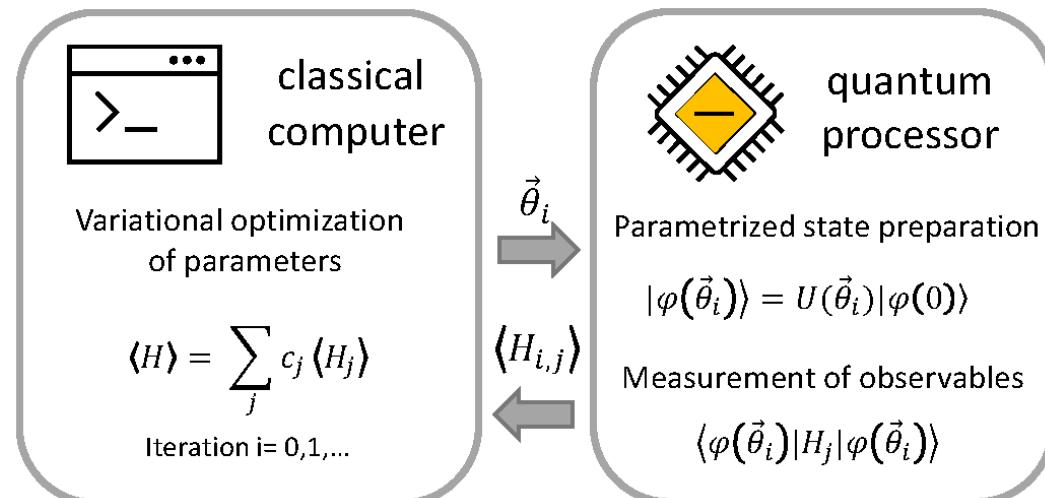


Fig. 4: Example of a graph representation of a quantum circuit with four qubits. The circuit contains gates not being part of the restricted native gate set \mathcal{N} .

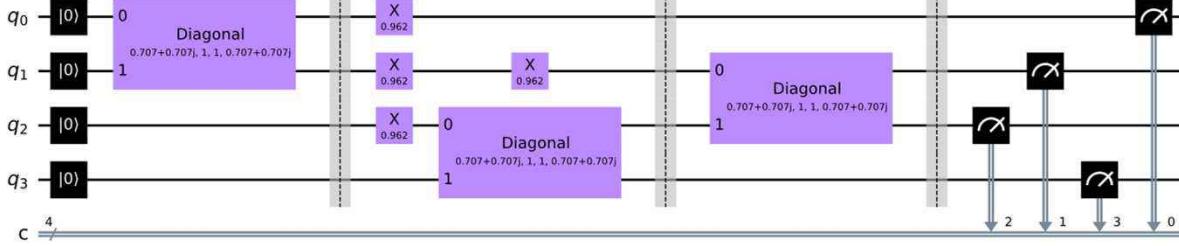


Circuit optimizer, acting with symbolic gates

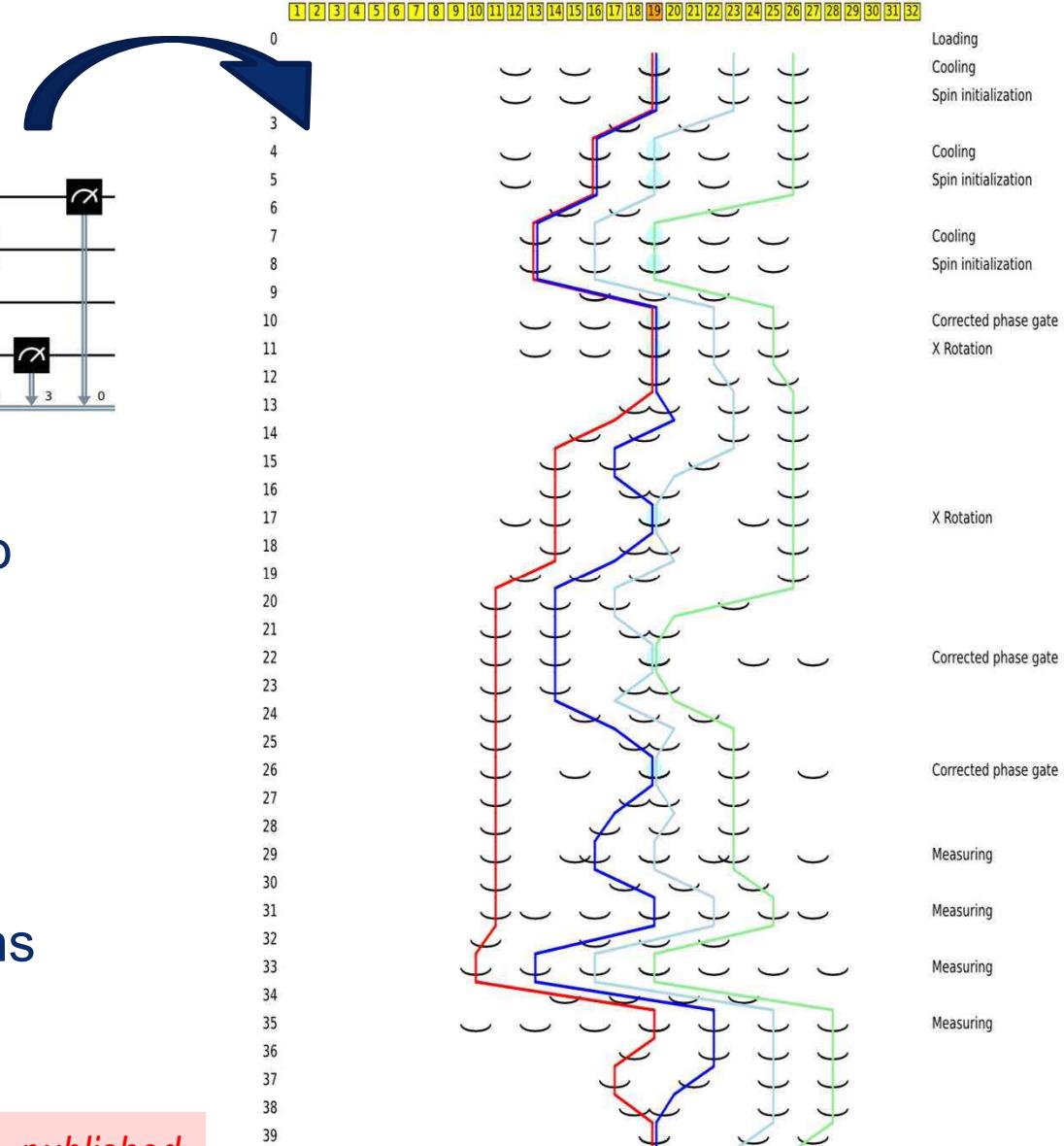
- Define and compile circuits including symbols
- Compilation only once
- Executions with different sets of parameters
- Same sequence in each repetition,
important in VQE



Shuttling compiler

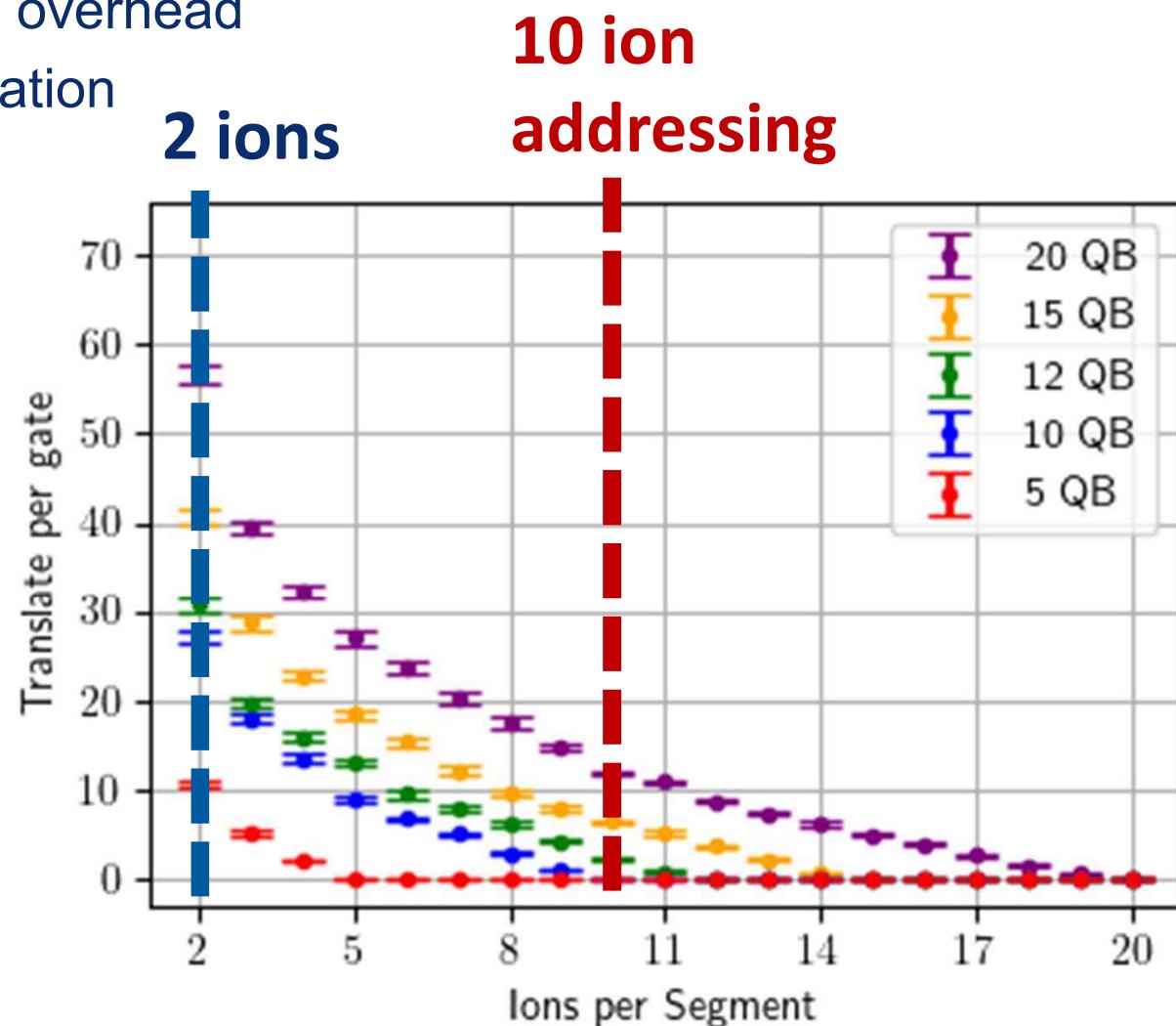
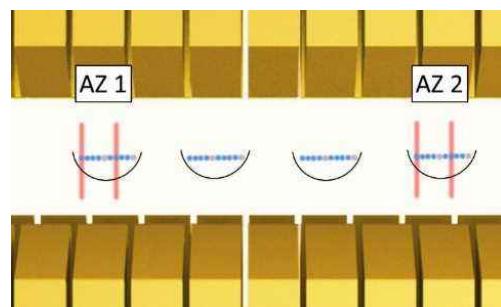


- Finds an initial mapping from qubits to ions heuristically
- Basic operations: translate, separate/merge, swap
- Currently: operations executed in the Laser Interaction Zone (LIZ) on ≤ 2 ions



Combine addressing and reconfiguration

- Drastic reduction of reconfiguration overhead
- Requires controlled multi-ion separation
- Remote reconfiguration operations
- Shuttle reduction: factor 5
- Separation reduction: factor 3
- SWAP reduction: factor 3
- IQuAn architecture

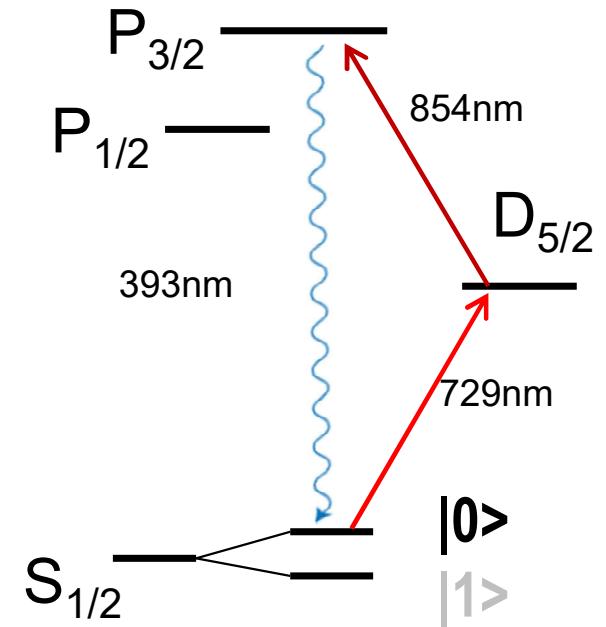
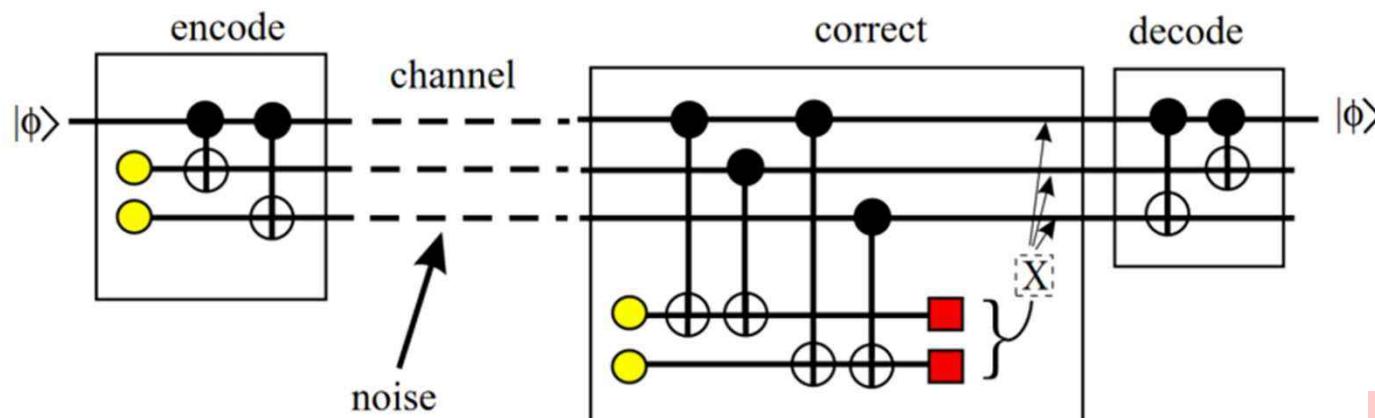


Mid-circuit qubit detection

- Illumination 729nm/854nm and 393nm photon detection
- Pros: no background UV light, no Doppler heating, little reabsorption, low qubit crosstalk

Applications:

quantum error correction, measurement-based QC
branching decisions,



Graham et al, arXiv:2303.10051
Motlakunta et al, arXiv:2306.03075

Hilder et al., Phys. Rev. X 12, 011032 (2022)

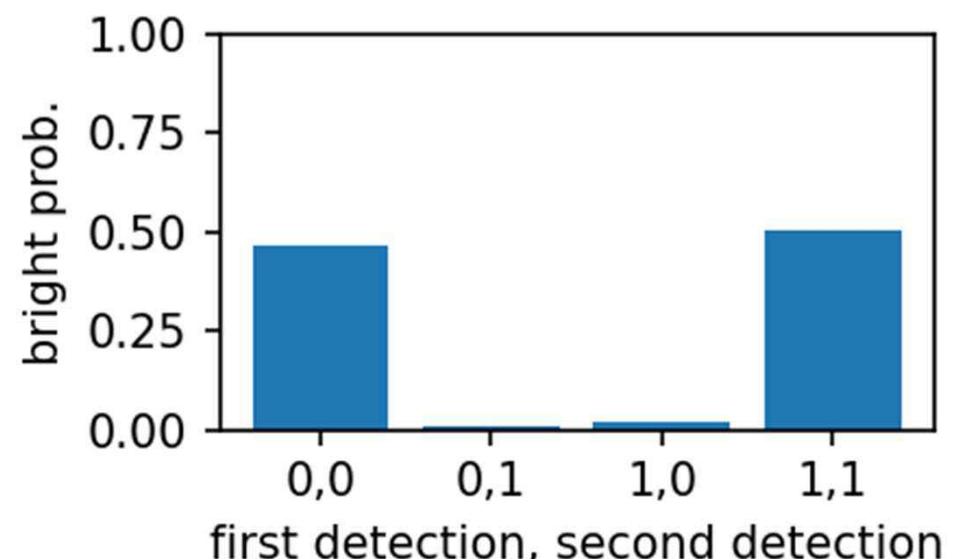
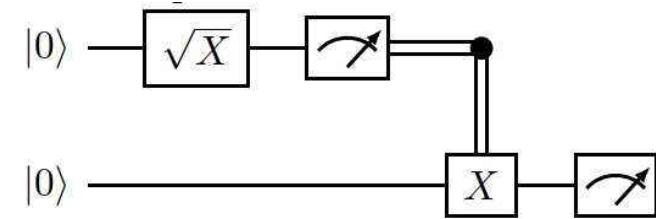
Realtime conditional reconfiguration operations

- FPGA SoC redesign
- PMT counter and thresholding on fmAWG
- Real-time decision logic

Proof-of principle: conditional qubit init. by
conditional shuttling to laser-interaction zone

Furthermore:
 Daemonic ergotropy with enhanced work
 extraction from quantum correlations

Francia, Goold, Plastina, Pernostro, *npj quant. Inf.* 3, 12 (2017)



IQuAn / ATIQ access

<https://www.iquan.de>



Consortium:
**Ionen-Quantenprozessor mit
HPC-Anbindung (IQuAn)**



JOHANNES GUTENBERG
UNIVERSITÄT MAINZ



Fraunhofer-Institut für Lasertechnik ILT



Fraunhofer-Institut für Angewandte Optik und
Feinmechanik IOF



Motivation

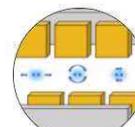
Scalable quantum computing will open completely new possibilities for many industrial and academic research and development efforts, comparable to emergence of integrated circuits in the 20th century.





Trapped-Ion

Atomic ions exhibit no fabrication variance. All qubits feature the same properties.



Shuttling-Based

Effective all-to-all connectivity due to dynamic register reconfiguration operations.



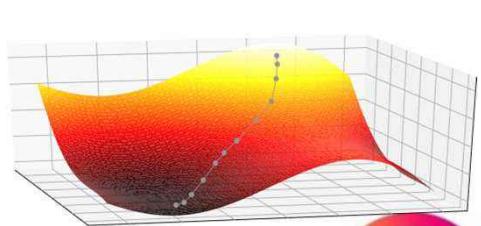
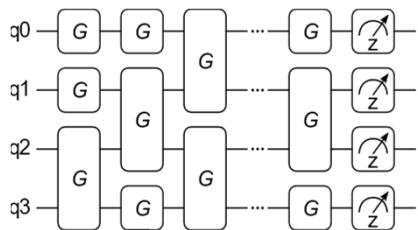
Laser-Driven

Laser-driven quantum gate operations performed at high fidelity.

→ Let's start computing ←

Applications and cooperations

VQE - Hybrid Variational Quantum Eigensolver

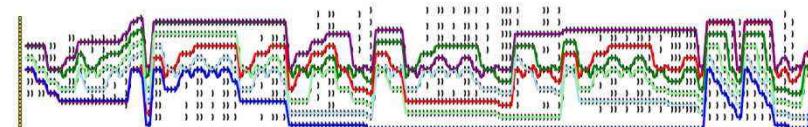


Determine the ground state of a molecule



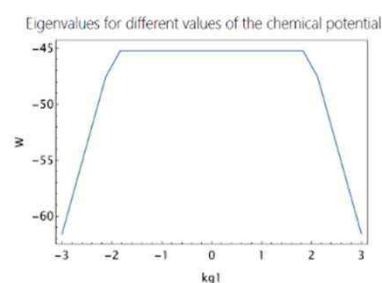
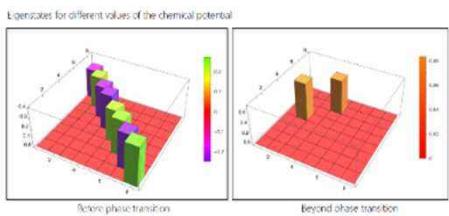
ParityQC Architecture

Map optimization problem to parallelizable design of four-qubit interactions



VQS for High-Energy Physics K. Jansen, DESY

Variational Quantum Simulation of Multi-Flavor Schwinger Model

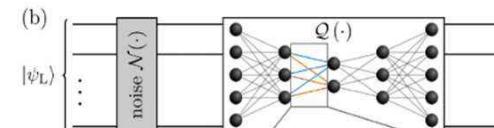
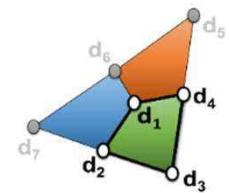


Beyond NISQ

T. Monz / M. Müller

Ongoing work on:

- QEC – Quantum Error Correction
- QAE – Quantum Auto Encoder
- Logic operations with logic qubits



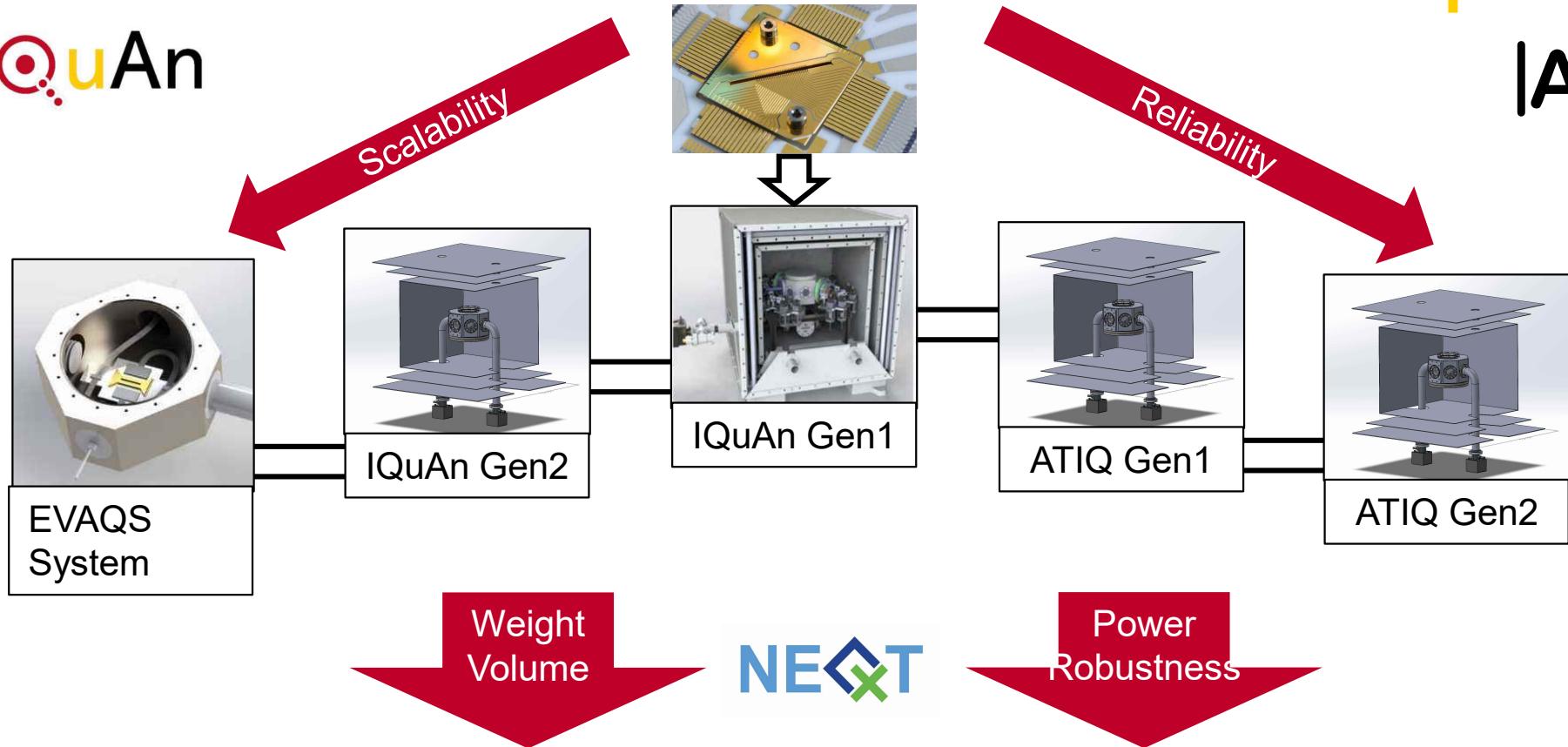
Mainz Quantum Computer Experiments



Bundesministerium
für Bildung
und Forschung

|IQuAn

|ATIQ+>



commercializing Quantum Computer

Startup NEQXT

- ❑ Fully integrated ion processor modules, fibre coupled
- ❑ Scalable to > 100 fully connected qubits
- ❑ Entire software stack & used case examples



Quantum Computing for User Applications



- ❑ Compact, modular FPGA controlled electronic units
- ❑ Clean room for custom SLE fabrication

<https://neqxt.org/>



Key figures in trapped ion QC



long-range Coulomb interaction

- Single shot read-out of spin state better than $1 - 10^{-4}$
- Single gate fidelity better than $1 - 10^{-4} \dots 10^{-5}$
- Two qubit gate fidelity $1 - 10^{-3} \dots 10^{-4}$
- Two-qubit gate operation times $\sim 30 \dots 100 \mu\text{s}$

Ion qubit entanglement
is relatively slow

Rydberg properties

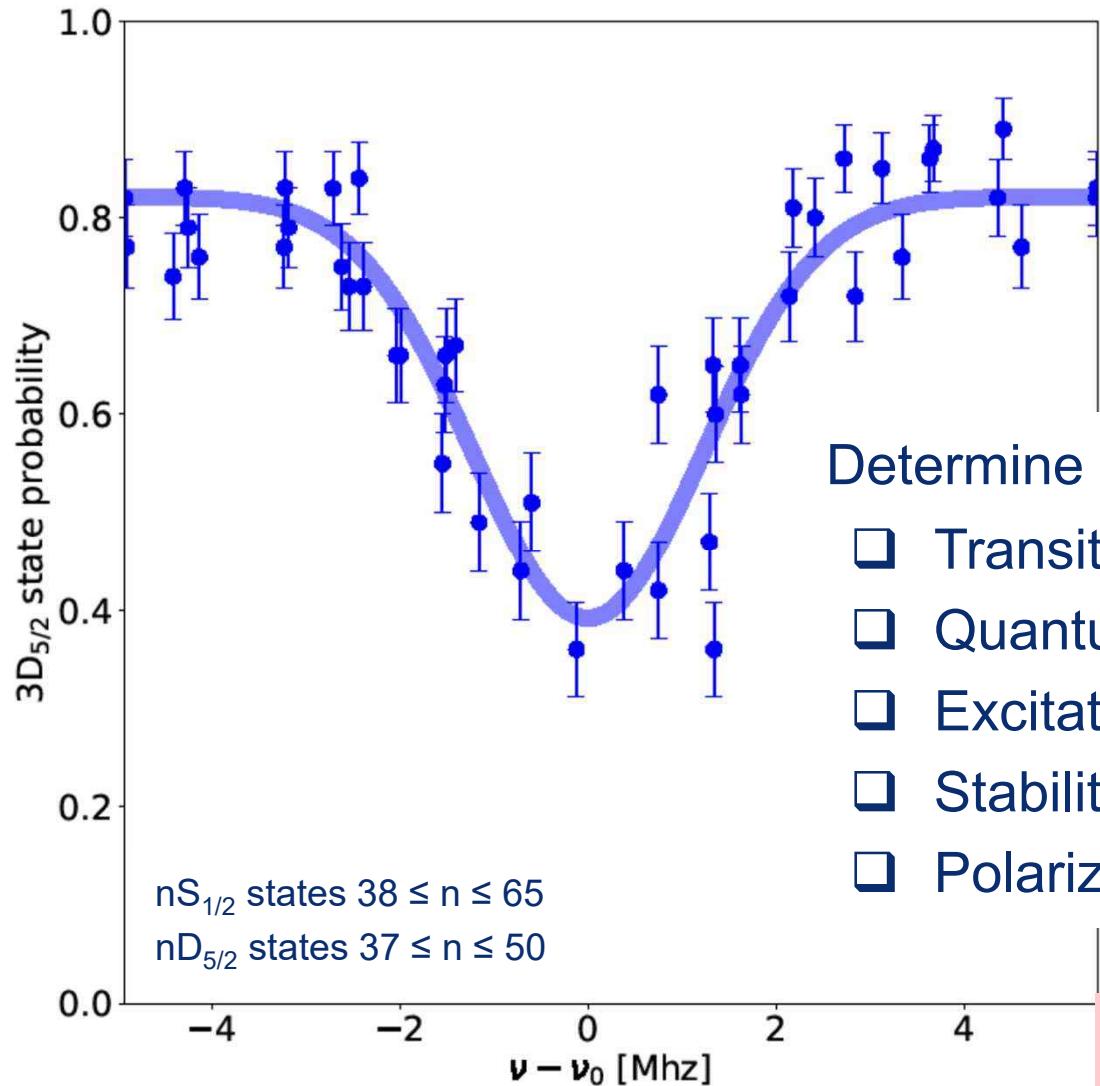
- Rydberg dipole blockade
- Rydberg polarizability - state-dependent effective ion mass

Zhang et al, Nat. 580, 345 (2020)
Saffman, Walker, M\"olmer, RMP 82, 2313 (2010)

Join advantages for ion trap qubits
with Rydberg excitations and interactions

Vogel et al, PRL 123, 153603 (2019)
Han et al., (2023)

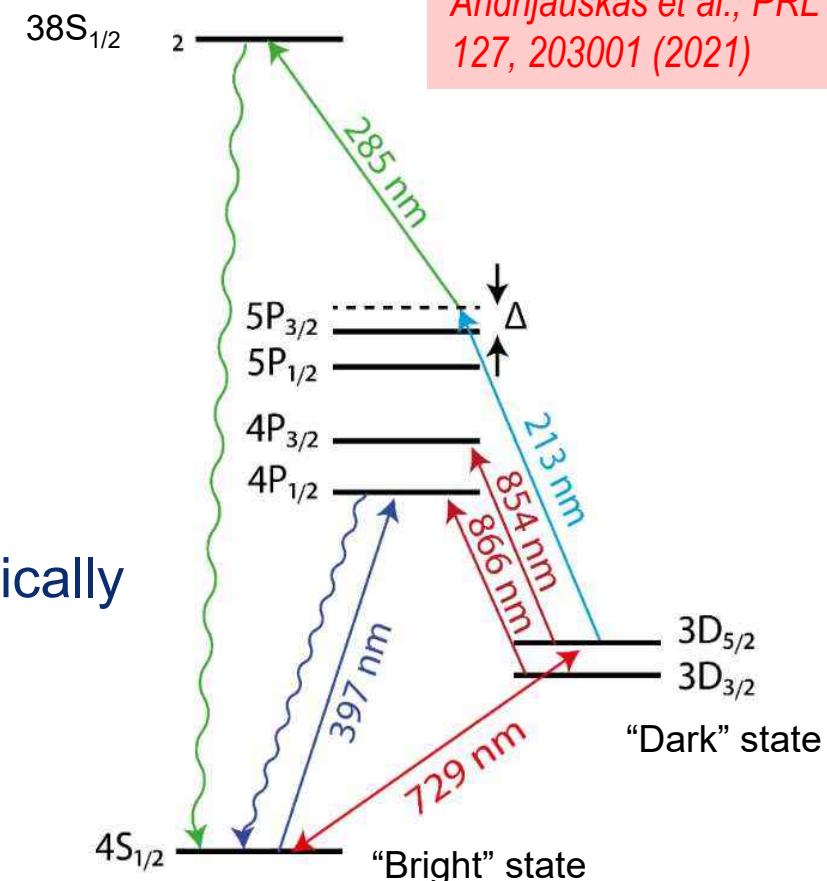
Rydberg excitation of a single ion



Determine spectroscopically

- Transition energy
- Quantum defect
- Excitation strength
- Stability in trap
- Polarizability

Niederländer et al,
NJP 25 033020 (2023)



Andrijauskas et al., PRL 127, 203001 (2021)
Schmidt-Kaler et al, NJP 13, 075014 (2011)
Feldker et al, PRL 115, 173001 (2015)
Higgins et al, PRX X 7, 021038 (2017)
Zhang et al, Nature 580, 345 (2020)

Polarizability → Trap frequency change

- Radial electr. field gradient much higher as axial

$$\gamma_{DC} = 4.69 \times 10^6 \text{ V/m}^2$$

$$\gamma_{RF} = 3.33 \times 10^8 \text{ V/m}^2$$

- Choose n → P(nS)
- Radial: 1.64MHz – 33.8kHz
Axial : 1.07MHz – 47Hz

$$\omega_x = \sqrt{\frac{2e^2\gamma_{RF}^2}{M^2\Omega_{RF}^2} - \frac{2e\gamma_{DC}(1+\epsilon)}{M} - \frac{2\mathcal{P}(\gamma_{RF}^2 + \gamma_{DC}^2(1+\epsilon)^2)}{M}}$$

$$\omega_y = \sqrt{\frac{2e^2\gamma_{RF}^2}{M^2\Omega_{RF}^2} - \frac{2e\gamma_{DC}(1-\epsilon)}{M} - \frac{2\mathcal{P}(\gamma_{RF}^2 + \gamma_{DC}^2(1-\epsilon)^2)}{M}}$$

$$\omega_z = \sqrt{\frac{4e\gamma_{DC}}{M} - \frac{16\mathcal{P}\gamma_{DC}^2}{M}} .$$

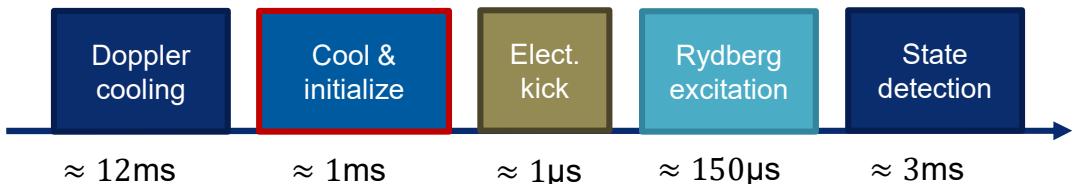


$$P(49S_{1/2}) = 1.3 \times 10^{-30} \frac{C \cdot m^2}{V}$$

	00>	01>	10>	11>
Rocking (MHz)	1.239	1.216	1.216	1.194
Rad. CM mode (MHz)	1.637	1.621	1.621	1.604

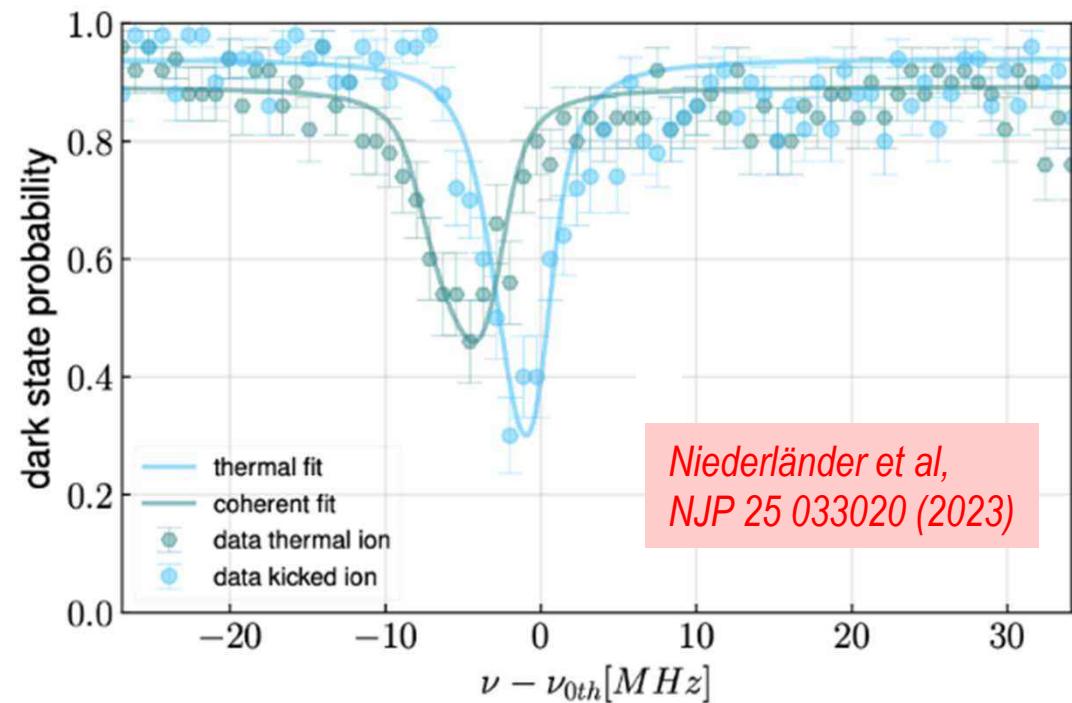
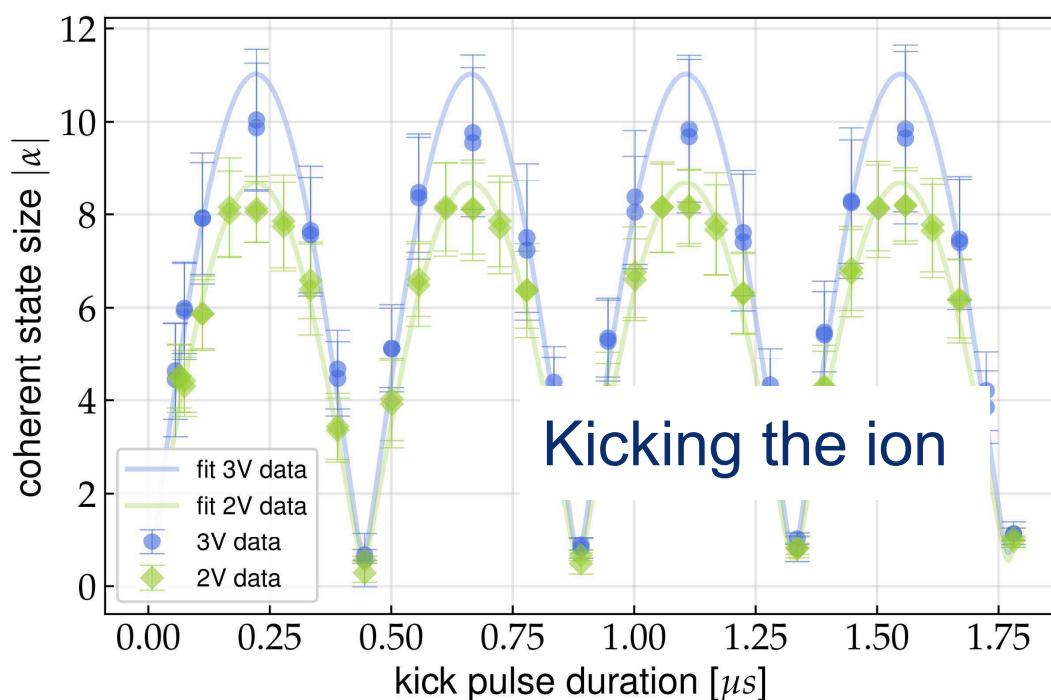
- Close the phase space trajectories with the properly chose kick sequence and get the right phase area – kick it back to the origin

Exploring the E-field in the trap

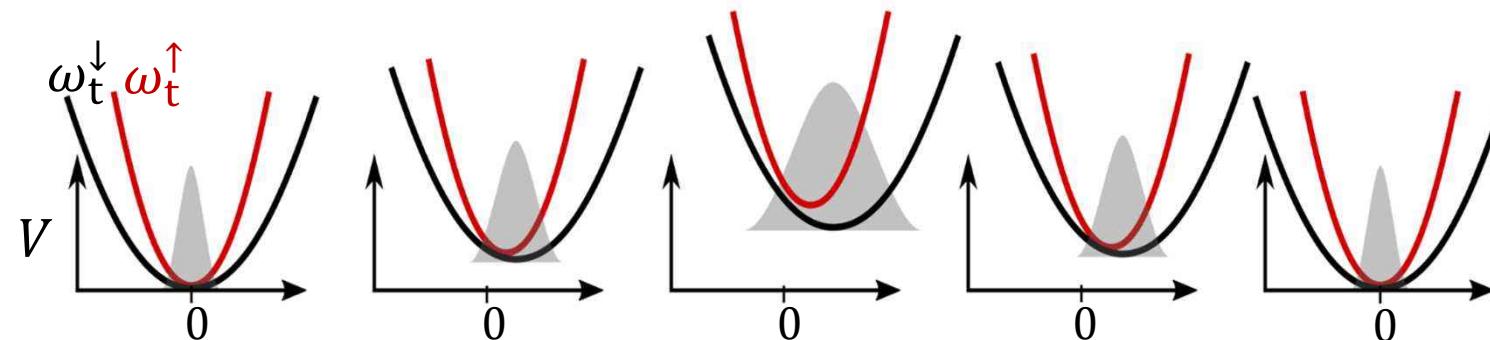


- Cool ion near ground state
- Generate coherent state of ion radial motion
- Sense interaction with electric field

- Observe shift due to polarizability



Kicking ion crystal for entanglement



Ripol et al., Phys. Rev. A 71, 062309 (2005), Steane, New J. Phys. 16, 053049 (2014), Schäfer et al, Nat. 555, 75 (2018), Shapira et al. Phys. Rev. A 101, 032330 (2020)

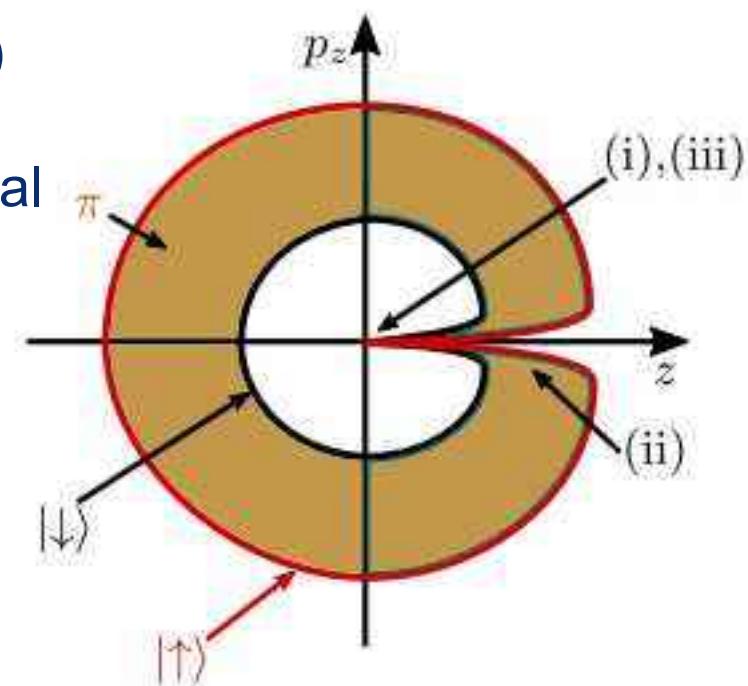
- Excite a superposition of $D_{5/2}$ (\downarrow) and Rydberg state (\uparrow)
- Apply electric kick (i)
- Rydberg polarizability results in **spin-dependent** potential
- Kick back (ii)
- Observe geometric phase

To do:

- Robustification against δV and $\delta \tau$
- all-to-all in $N=10$ ion crystal

Vogel et al, PRL123, 153603 (2019)

Bao et al, (2023)



Conclusion – Rydberg excitations of trapped ions

- New platform is established experimentally
- Spectroscopy groundwork done
- Polarizability tuning by MW dressing and trap E-fields
- Pathways towards sub- μ s high fidelity gate operation
- Rydberg excitations may contribute to the ion qubit toolbox

First Ryd. Ion ever: [Feldker et al, PRL 115, 173001 \(2015\)](#)

Fast gate proposal: [Vogel et al, PRL 123, 153603 \(2019\)](#)

Spectroscopy: [Andrijauskas et al, PRL 127, 203001 \(2021\)](#)

Rydberg ion review: [Mohberi et al, Adv. At. Mol. Opt. Phys. 69, 233 \(2020\)](#)

Quantum Computing Team @ JGU Mainz

Want to join?



Jonas Vogel



Daniel Pijn



Janine Hilder



Björn Lekitsch



Ulrich Poschinger



Ferdinand Schmidt-Kaler



Felix Stopp



Jan Müller



Alexander Stahl



Maximilian Orth



Christian Melzer



Janis Wagner



Alexander Müller



Robin Strohmaier



Daniel Wessel



Diego Olvera Millán



Andreas Conta



Sahori Jiménez



Helin Özal



Dario Moreira



Pauline Wagner



Lukas Klein



Fabian
Kreppel



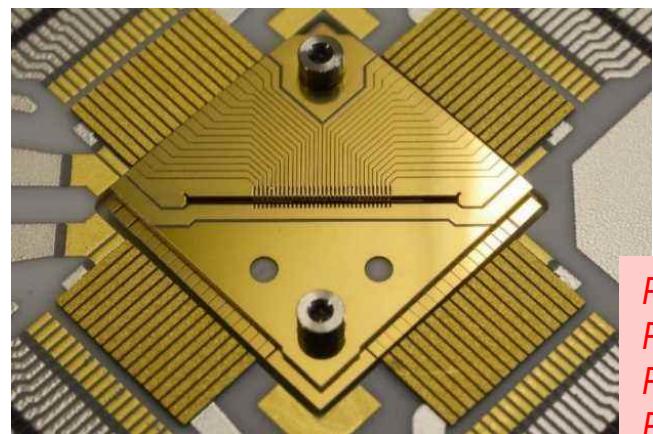
André
Brinkmann

Quantum technologies with trapped ions @QUANTUM

www.quantenbit.de

Want to join?

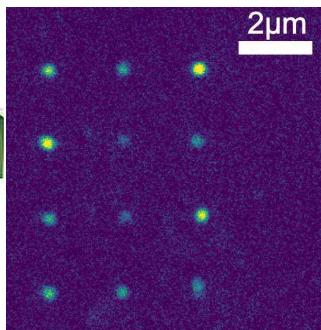
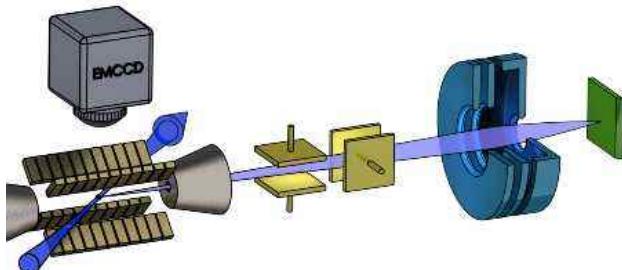
Universal trapped-ion Quantum Computer



PRL 119, 150503
PRX 7, 031050
PRX 7, 041061
PRX 12, 011032

Single ions delivered
for solid state QC

PRL 117, 043001
PRL 123, 106802
Qu. Sci. Techn. 7, 034002



Rydberg
ions



PRL 115, 173001
PRL 123, 153603
Adv. At. Mol. Opt. Phys. 69, 233
PRL 127, 203001
NJP 25, 033020

Sci. 352, 325
PRL 123, 080602
PRL 128, 110601



Ion heat engines

PRL 116, 183002
PRL 126, 173602
PRL 127, 143602
PRR 5, 013163



Photon correlations $g^{(2)}(x, \tau)$

Exotic ions: H^+ / Th^+



PRA 99, 023420
NJP 24, 043028
PRX Q3, 010330

Optical angular momentum

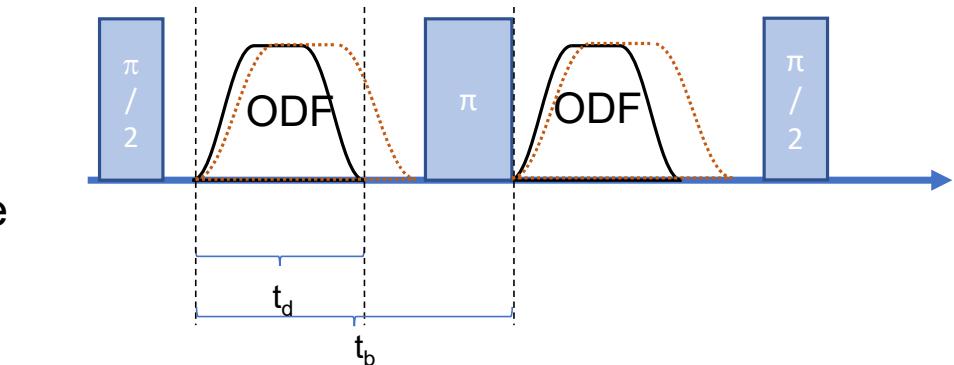
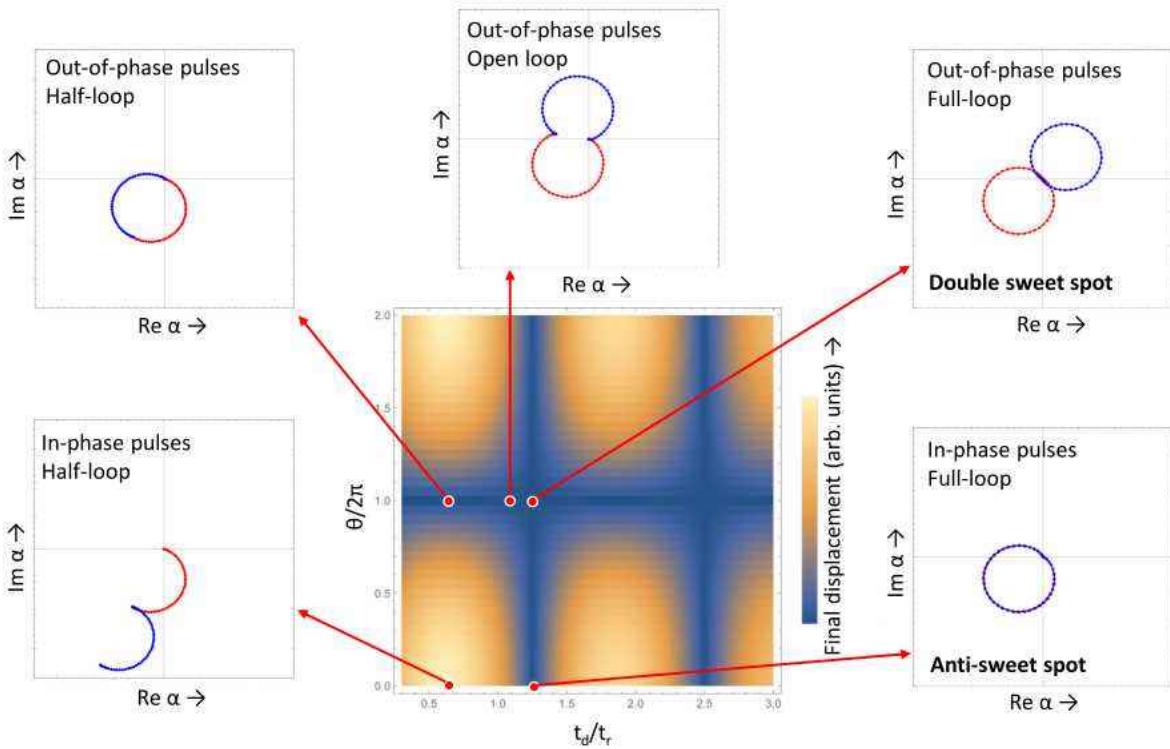


Nat. Com. 7, 12998
PRL 119, 253203
JOSAB 36, 565
PRL 127, 143602
PRL 129, 263603

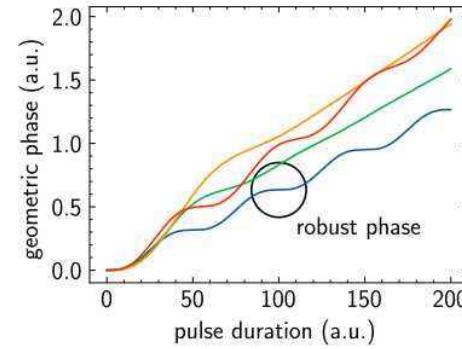
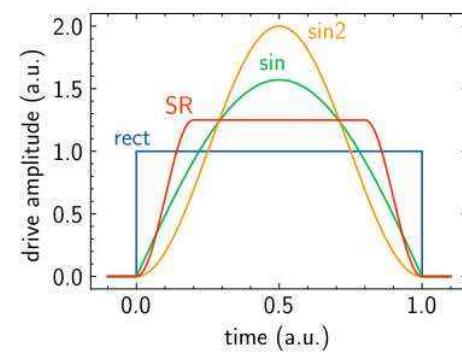
Spin-echo gate operation

- perform spin echo for spin-asymmetric error sources
- minimize residual displacement with phase of 2nd pulse
- back to initial phonon state

robust in phase **and** in duration

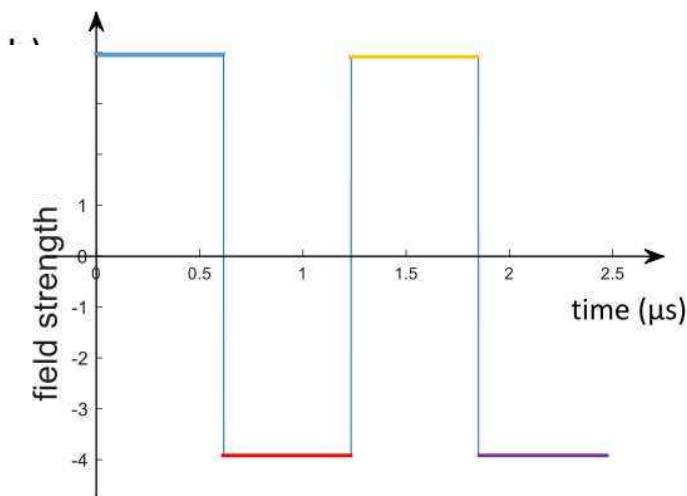


- Pulse shaping
- Smooth rectangular (SR) is optimal
- Robust in duration
- Low excitation of other (spectator) modes



Radial 4-kick gate

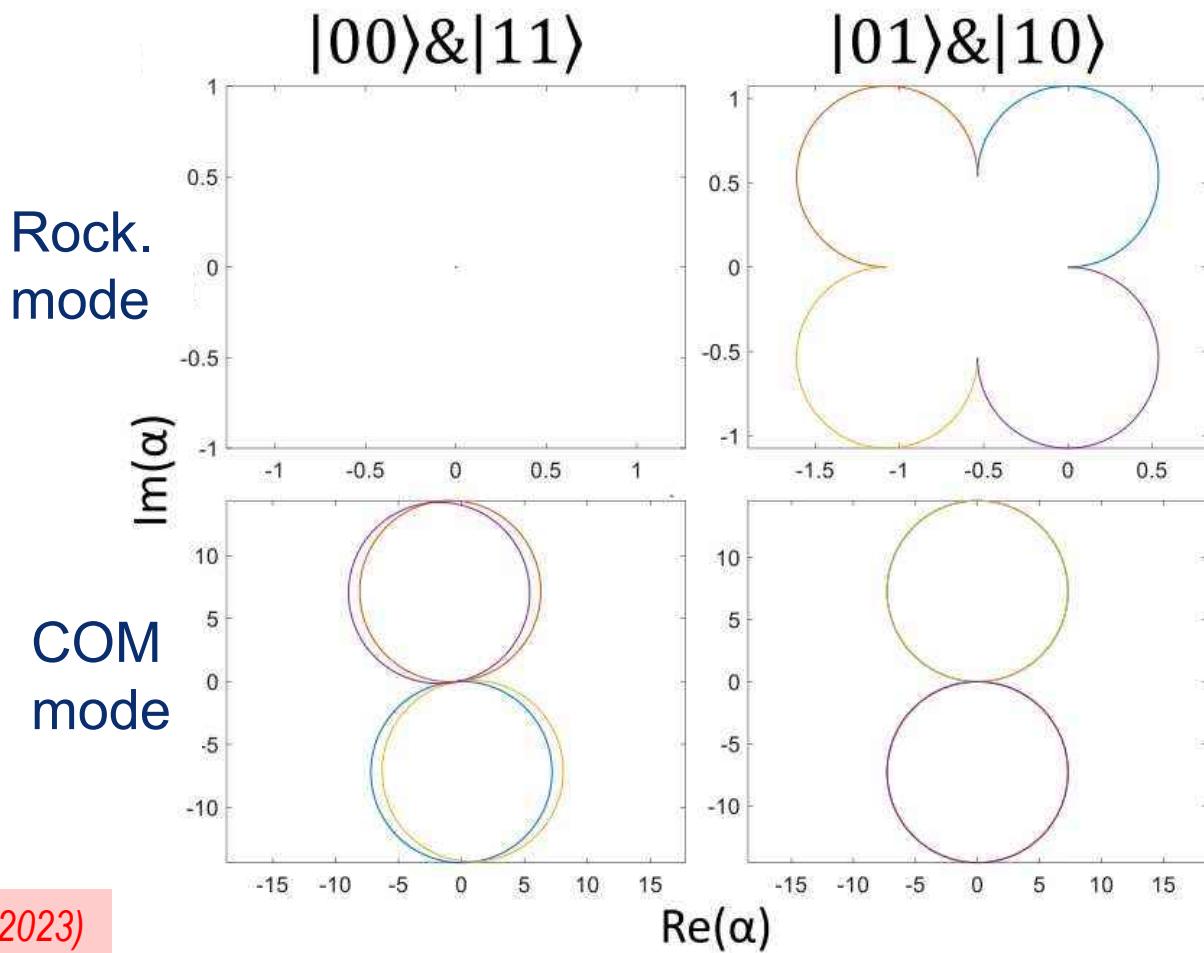
- ❑ Chose 49p for better lifetime
- ❑ Spin-echo like



To do:

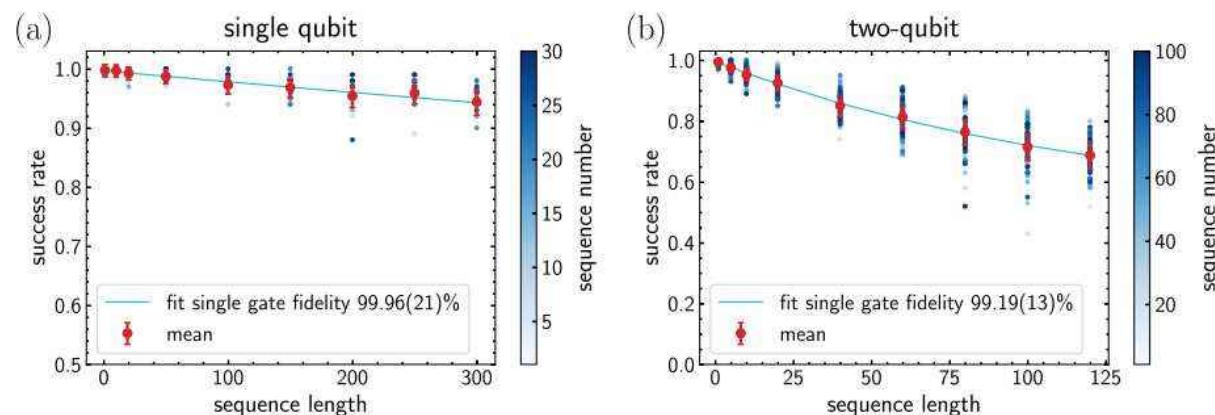
- ❑ Robustification against δV and $\delta \tau$
- ❑ all-to-all in N=10 ion crystal

Phase space trajectories:

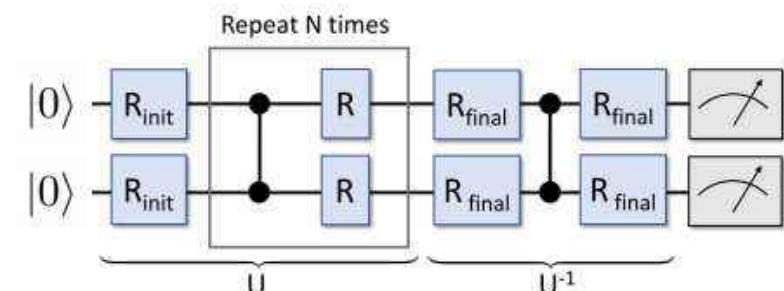
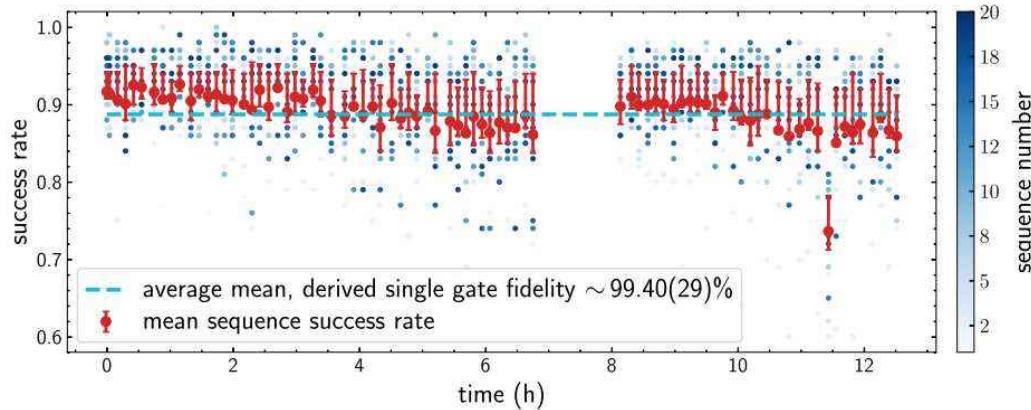


Characterize the gate

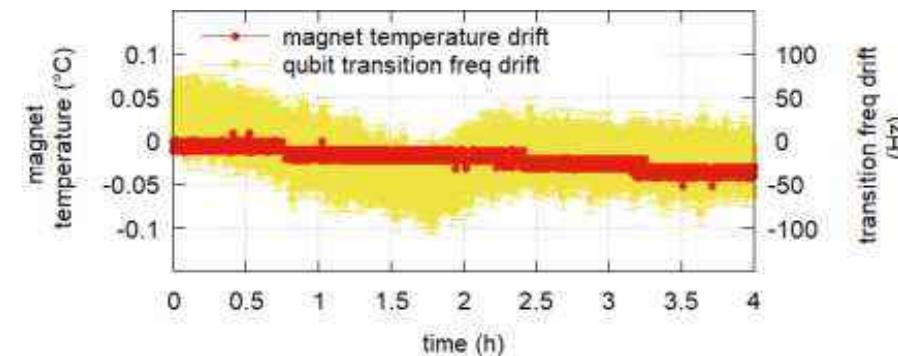
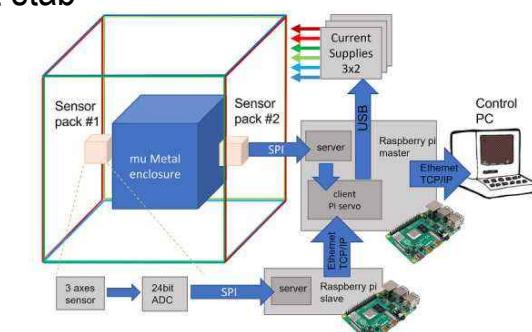
- Cycle benchmarking is able to sense
- small gate imperfection in the presence of SPAM (state preparation and readout errors)



- Long term stability, here 20 gate sequence



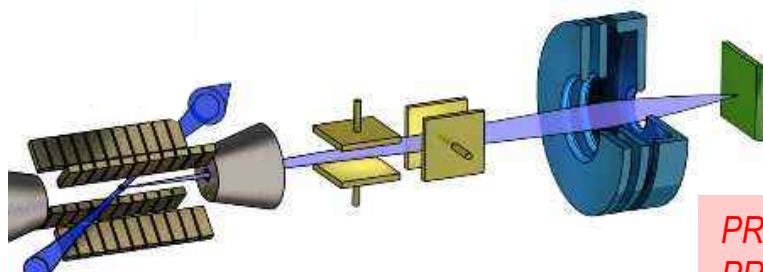
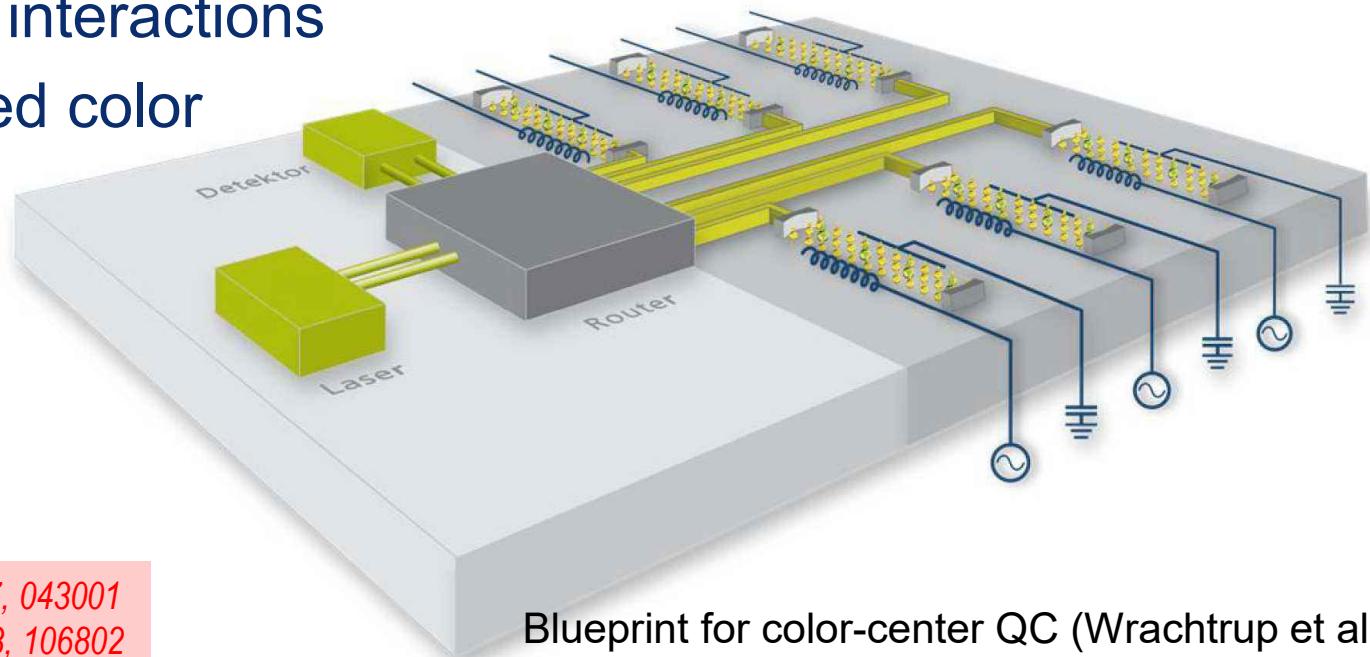
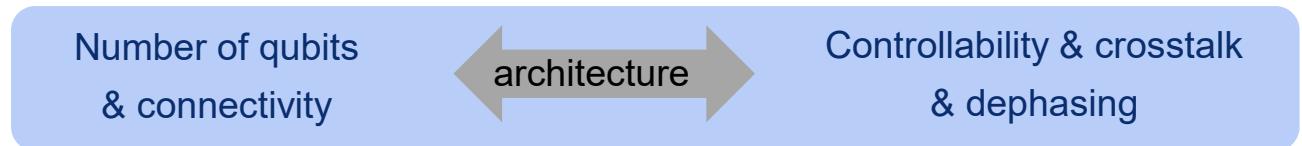
- Fighting 13T ramps from the basement with 2-layer μ -shield and active comp.
- Permanent magnet quant. B field thermal drift
- < 80Hz qubit stab



Finding a compromise:

Architecture with **different levels connectivity** of processor nodes,
here color center qubits:

- Spin-spin and cavity-mediated spin interactions
- Cavity-cavity far-distance interactions
- Eventually single implanted color centers

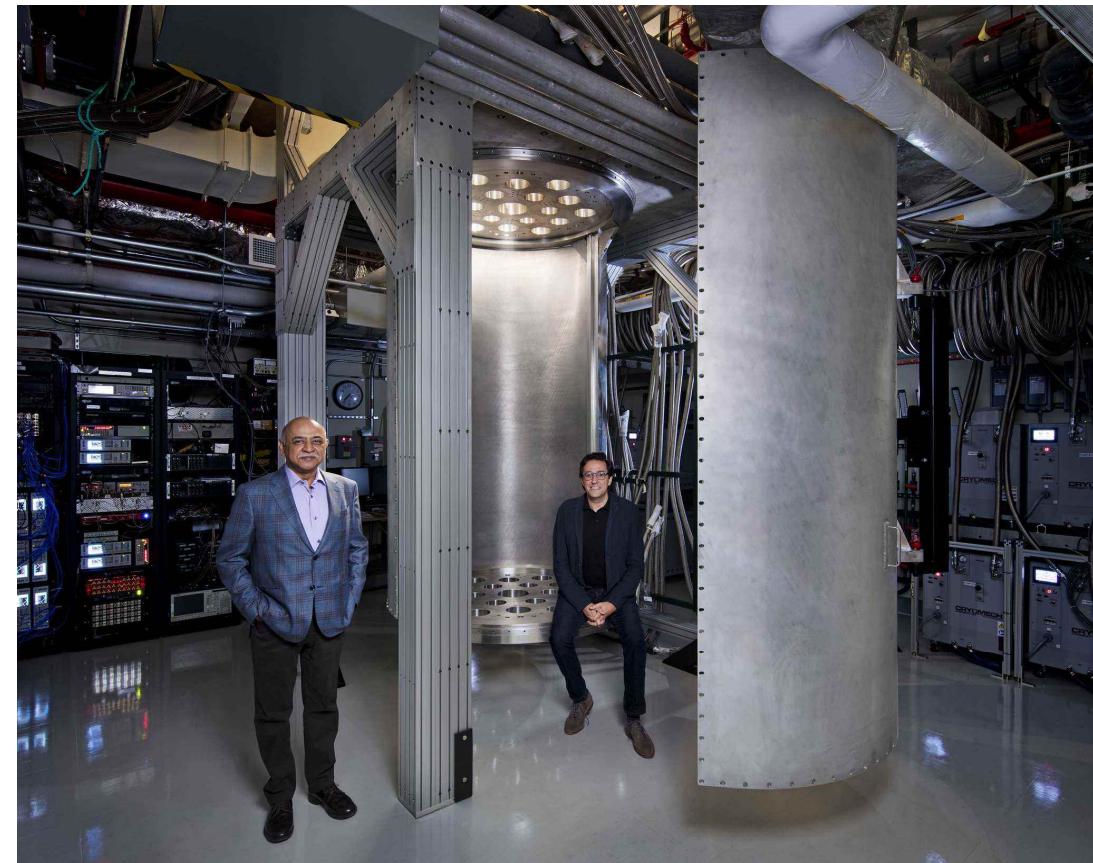


PRL 117, 043001
PRL 123, 106802

Blueprint for color-center QC (Wrachtrup et al.)

Addressability and scaling

Each qubit needs several control wires, down to the cryostate @ 20mK



Various platforms for quantum computers



Trapped ion qubits: highest fidelities for gates and qubit preparation, longest coherence



Superconduction circuits: highest speed in gates and qubit detection



Neutral atoms: highest number of qubits



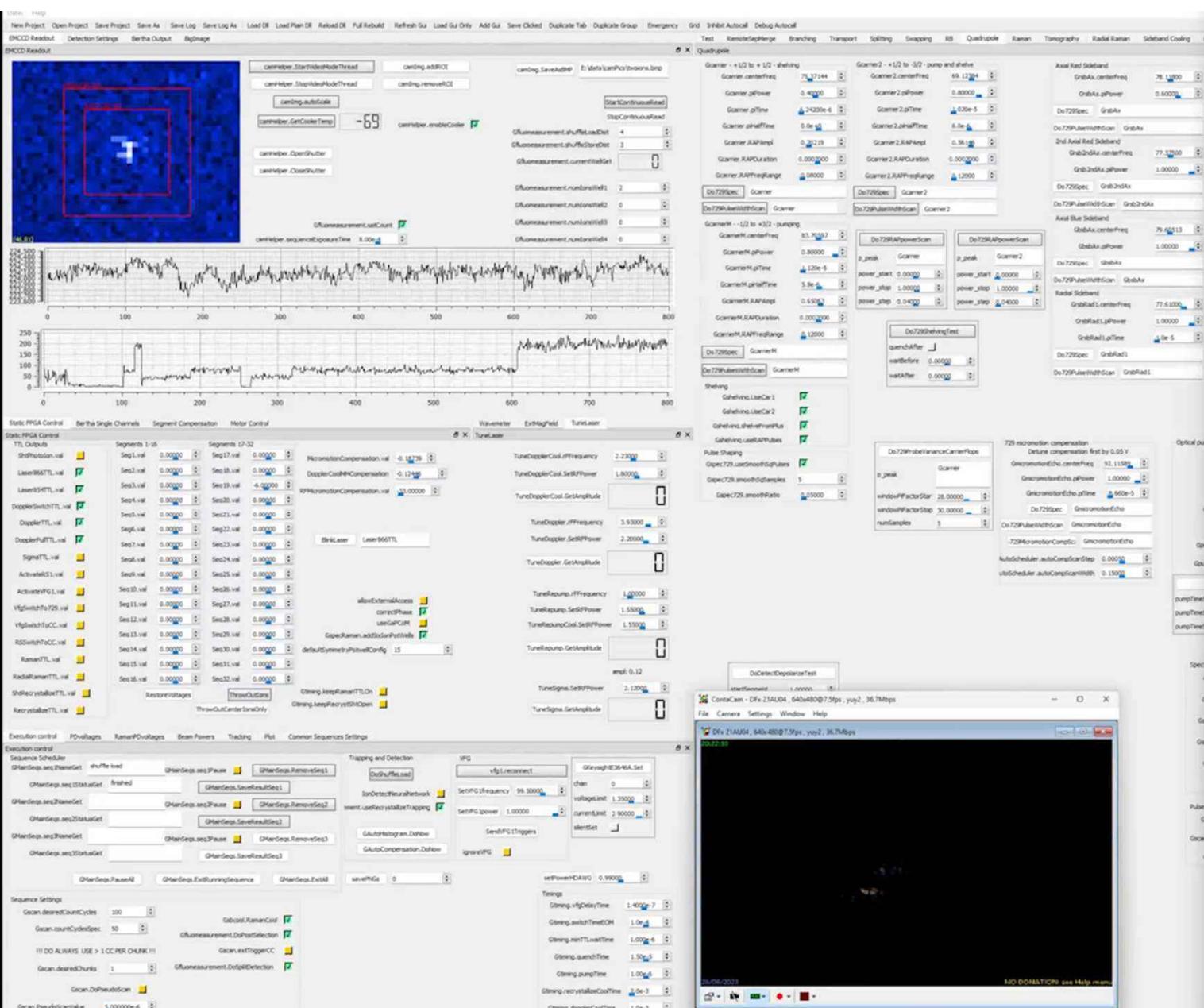
Photonic devices: fast, interconnectivity of nodes



Quantum dots, single donors: connecting to solid state processor fab. technology







jupyter UMZ_Demo (unseen changes) Logout

File Edit View Insert Cell Kernel Help Trusted qiskit O

UMZ Qiskit Interface

```
In [16]: from qiskit import QuantumCircuit
from numpy import pi
from umz_qiskit_backend.qiskit_backend import RedTrapBackend, UmzSimulatorBackend
from qiskit.visualization import plot_histogram
from itertools import product as cart_prod

def get_data(job):

    qubits = job.result()["result"][0]["labels"]
    all_states = cart_prod(["0", "1"] for q in qubits)
    all_states = [".".join(state) for state in list(all_states)] 

    data = job.result()["result"][0][{"measurements"}].copy()

    for state in all_states:
        if not state in data:
            data[state] = 0

    return data

In [17]: backend = RedTrapBackend()
```

```
In [18]: backend_sim = UmzSimulatorBackend()
```

```
In [19]: circ = QuantumCircuit(2)
circ.rx(pi/2, 0)
circ.rx(pi/2, 1)
circ.rzz(pi/2, 0, 1)
circ.rx(pi/2, 0)
circ.rx(pi/2, 1)

circ.measure_all()
print(circ)
print(circ.qasm())
```

```
In [20]: n = 1000
```

```
In [21]: job = backend.run([circ], shots=n)
job_sim = backend_sim.run([circ], shots=n)

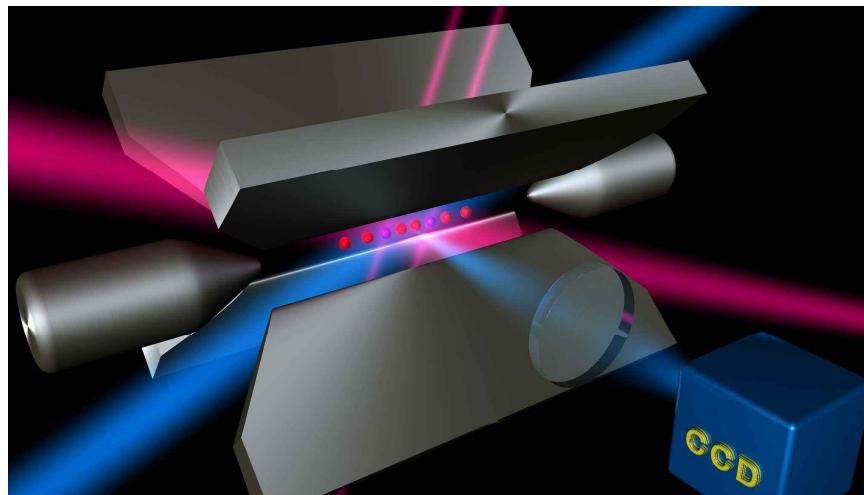
print(job.result())
print(job_sim.result())
```

```
In [22]: data = get_data(job)
data_sim = get_data(job_sim)

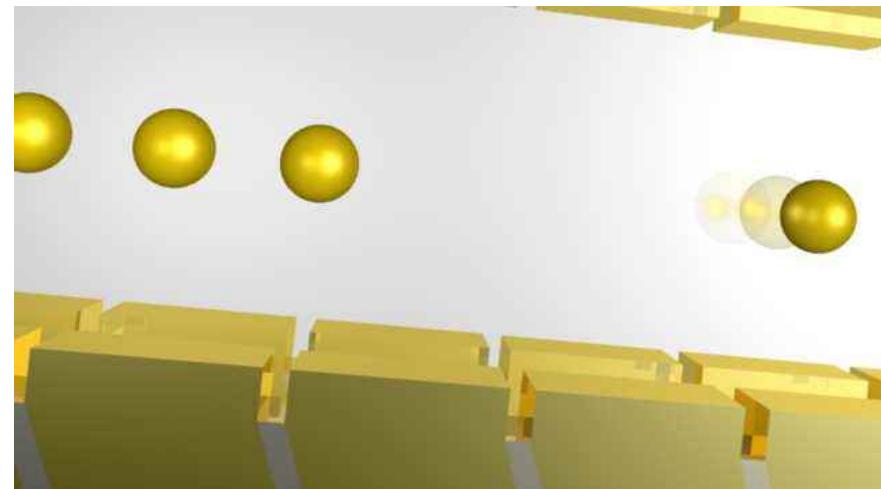
plot_histogram([data, data_sim], legends=["RedTrap", "Simulator"])
```

```
In [ ]:
```

Linear crystal processor



Quantum-CCD architecture



- Static trapped ion registers >20 qubits
- Individual single ion addressing for gates

- Segmented micro trap allows for controlling the ion positions

Nägerl, et al, PRA 60, 145 (1999)

Friis, et al, Phys Rev X. 8 021012 (2018)

Korenblit et al, NJP 14, 095024 (2012)

Egan et al., Nat. 598, 281 (2021)

Kielpinski et al., Nat. 417, 709 (2002)

Kaustal et al, Adv. At. Mol. Opt. Phys. 69, 233 (2020)

Ryan-A. et al, Phys. Rev. X 11, 041058 (2021)

Hilder et al., Phys. Rev. X 12, 011032 (2022)

Multi-Flavor Schwinger Model VQE



We adopt a lattice formulation with Kogut-Susskind staggered fermions [36]. In the temporal gauge, and in absence of a background field, the Hamiltonian for F flavors on a lattice with spacing a and N sites reads

$$H = -\frac{i}{2a} \sum_{n=0}^{N-2} \sum_{f=0}^{F-1} (\phi_{n,f}^\dagger e^{i\theta_n} \phi_{n+1,f} - \text{H.c.}) \\ + \sum_{n=0}^{N-1} \sum_{f=0}^{F-1} [m_f (-1)^n + \kappa_f] \phi_{n,f}^\dagger \phi_{n,f} \\ + \frac{ag^2}{2} \sum_{n=0}^{N-2} L_n^2. \quad (1)$$

Banuls, et al, PRL 118, 071601 (2017)

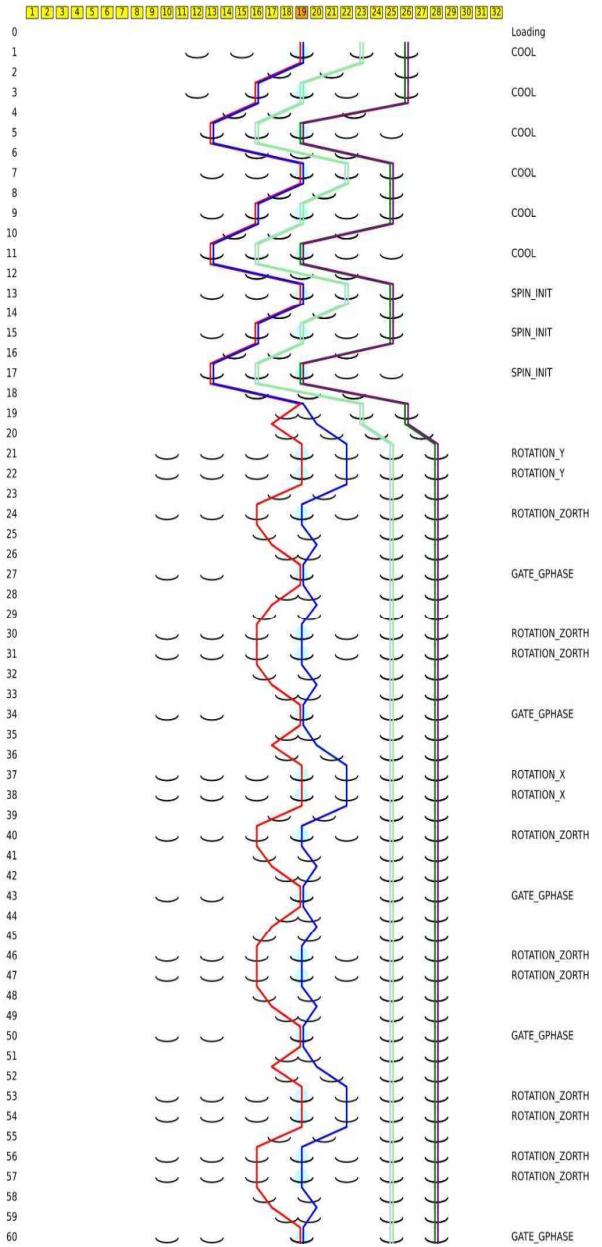
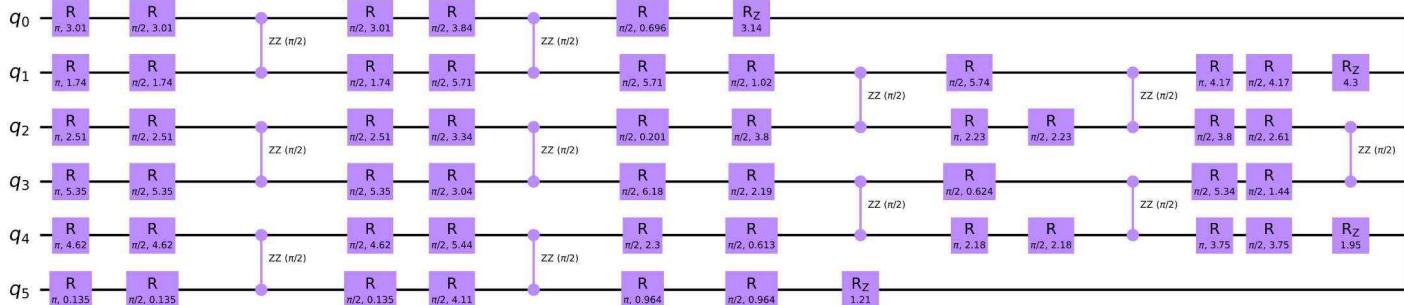
- Wigner transformation in circuit

$$W = 2\sqrt{x} \left(\frac{\kappa_0}{g} + \frac{\kappa_1}{g} + \frac{\kappa_2}{g} + \frac{3}{2\sqrt{x}} \right) \mathbb{1} + \sqrt{x} \left(\frac{m_0}{g} + \frac{\kappa_0}{g} + \frac{3}{2\sqrt{x}} \right) \sigma_0^z \\ + \sqrt{x} \left(\frac{m_1}{g} + \frac{\kappa_1}{g} + \frac{3}{2\sqrt{x}} \right) \sigma_1^z + \sqrt{x} \left(\frac{m_2}{g} + \frac{\kappa_2}{g} + \frac{3}{2\sqrt{x}} \right) \sigma_2^z \\ + \sqrt{x} \left(\frac{\kappa_0}{g} - \frac{m_0}{g} \right) \sigma_3^z + \sqrt{x} \left(\frac{\kappa_1}{g} - \frac{m_1}{g} \right) \sigma_4^z + \sqrt{x} \left(\frac{\kappa_2}{g} - \frac{m_2}{g} \right) \sigma_5^z \\ + \frac{1}{2} \sigma_0^z \sigma_1^z + \frac{1}{2} \sigma_0^z \sigma_2^z + \frac{1}{2} \sigma_1^z \sigma_2^z + \frac{x}{2} \sigma_0^x \sigma_1^z \sigma_2^z \sigma_3^x + \frac{x}{2} \sigma_0^y \sigma_1^z \sigma_2^z \sigma_3^y \\ + \frac{x}{2} \sigma_1^x \sigma_2^z \sigma_3^z \sigma_4^x + \frac{x}{2} \sigma_1^y \sigma_2^z \sigma_3^z \sigma_4^y + \frac{x}{2} \sigma_2^x \sigma_3^z \sigma_4^z \sigma_5^x + \frac{x}{2} \sigma_2^y \sigma_3^z \sigma_4^z \sigma_5^y.$$

- High-energy Hamiltonian H
- Minimal model: three flavours and two Fermions
- Quantum processor delivers $\langle W \rangle$ dep. on chem. potential & masses
- Classical minimum search
- Learn about flavour phases and transitions

Multi-Flavor Schwinger circuit for W

- ❑ Enter openquasim as python code for 6 qubits
 - ❑ Optimize quantum circuit
 - ❑ Convert into our native gate set
 - ❑ Generate shuttling sequence



Rydberg energies and quantum defect

- nS_{1/2} states 38 ≤ n ≤ 65
- nD_{5/2} states 37 ≤ n ≤ 50
- Ionization energy I⁺⁺=2 870 575.582(15) GHz
- Quantum defects:

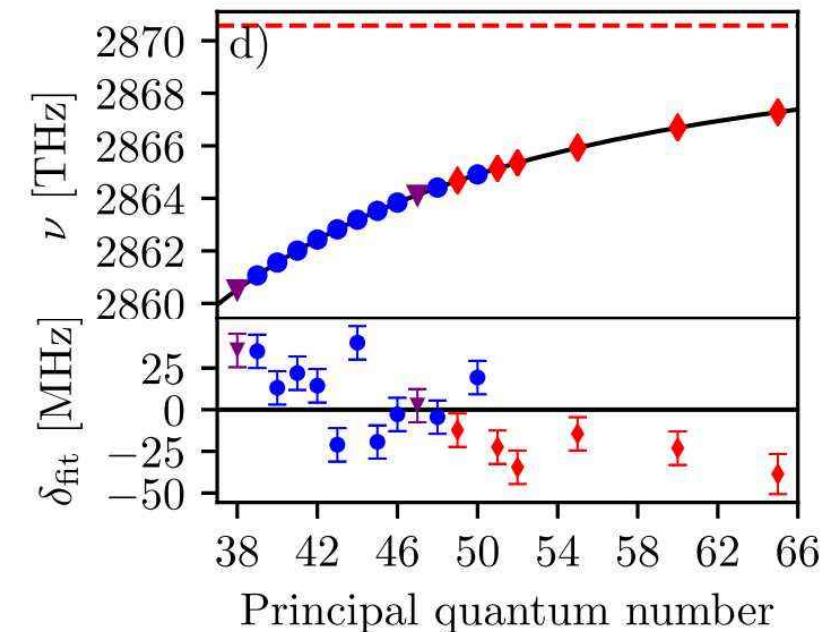
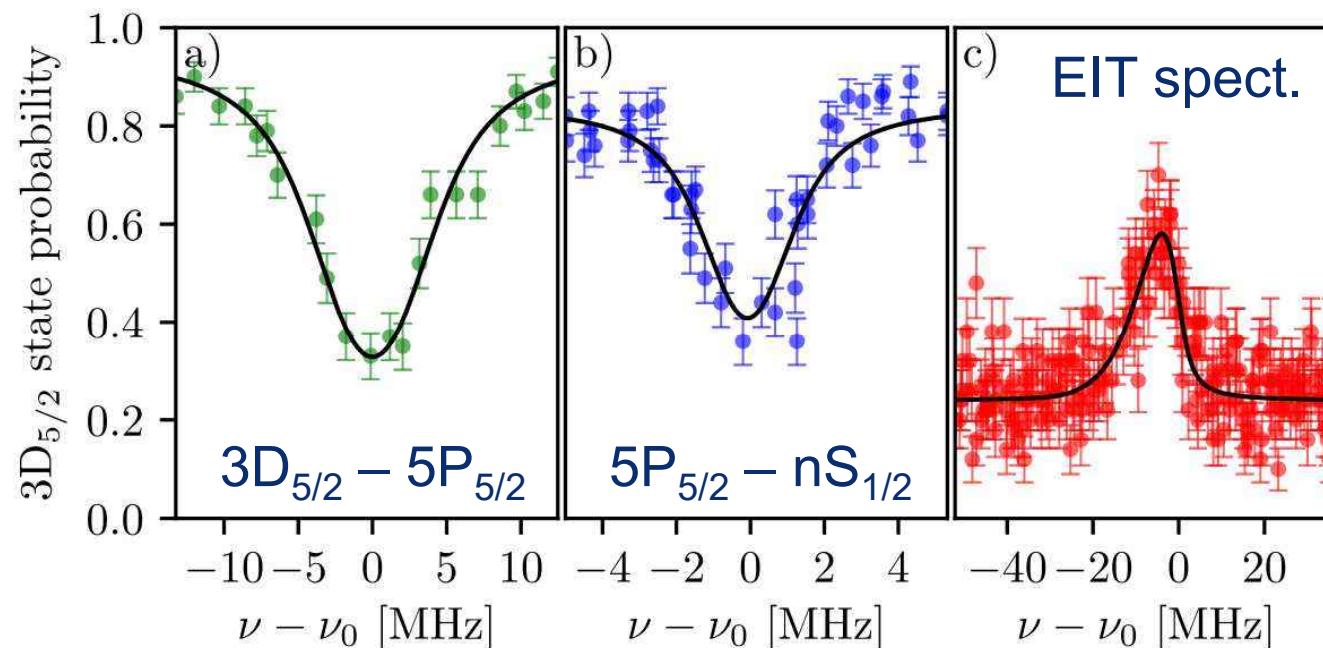
$$\mu^S = 1.802995(5) \quad \mu^D = 0.626888(9)$$

x60

$$E_{n,l,j} = I^{++} - \frac{Z^2 R^*}{(n - \mu(E))^2} +$$

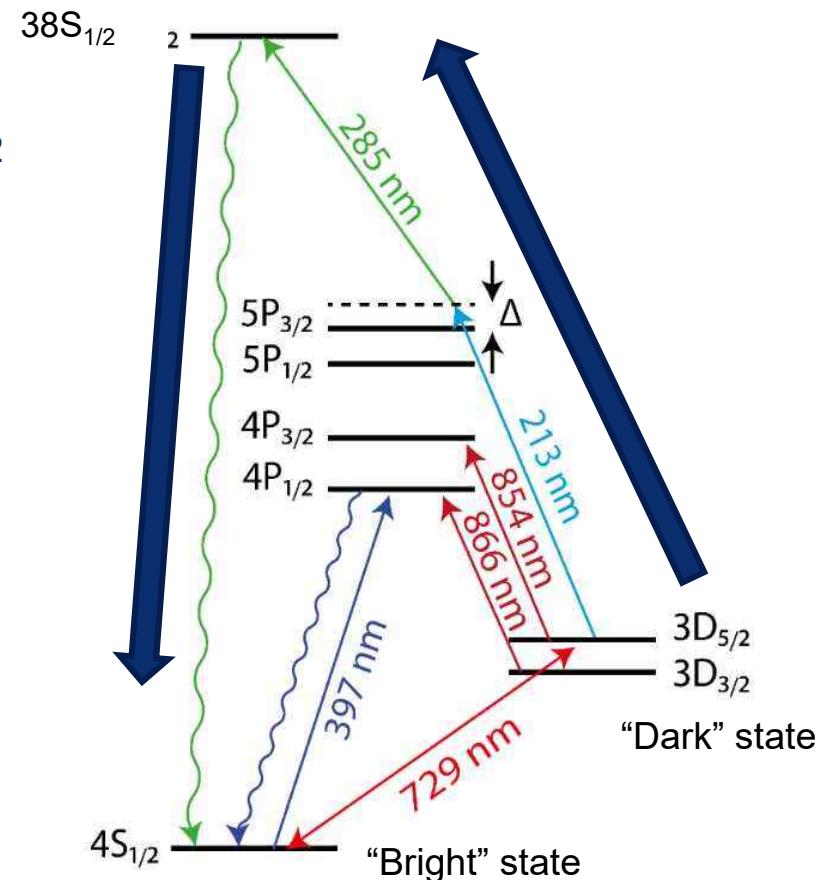
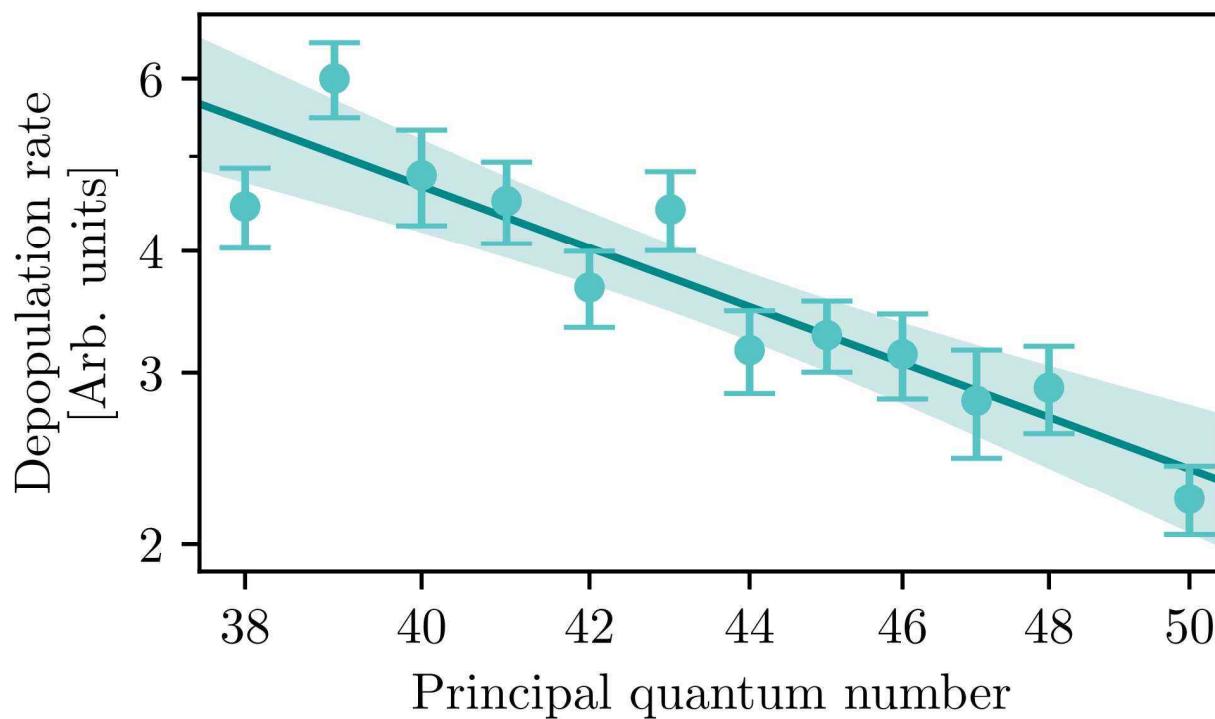
$$\frac{Z^4 \alpha^2 R^*}{(n - \mu(E))^3} \left[\frac{3}{4(n - \mu(E))} - \frac{1}{(j + 1/2)} \right]$$

Rydberg Ritz formula



Rydberg-induced depopulation rate

- Rate up determined by matrix dipole moment $\sim n^{-3/2}$
- Rate down determined by Rydberg life time
- Resulting depopulation rate $\sim n^{-3.0(0.4)}$
- Agreement with expected n-scaling



Andrijauskas et al., PRL
127, 203001 (2021)

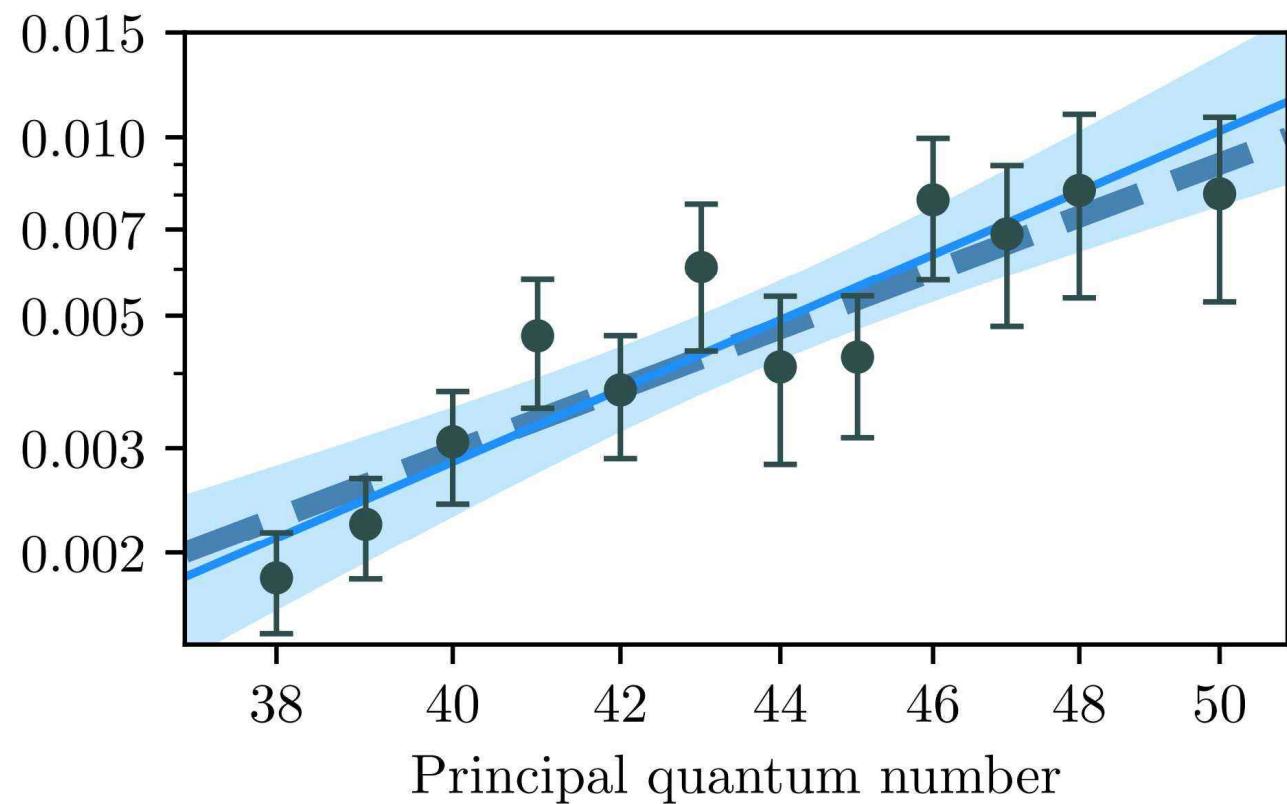
Adv. At. Mol. Opt. Phys. 69, 233
arXiv:2009.01070

Rydberg ion stability in the trap

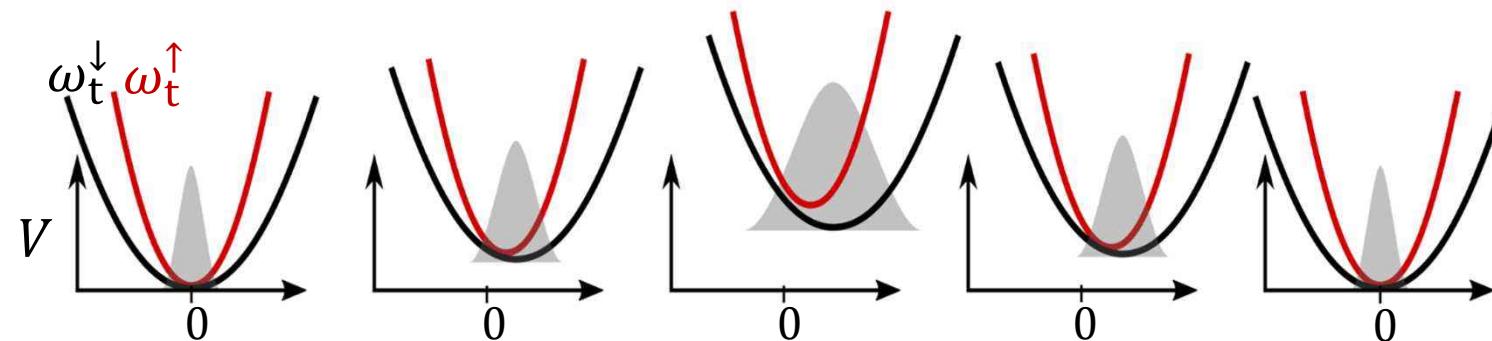
- Loss rates of $1.8 \dots 8 \times 10^{-3}$
- Double-ionization
dominates „loss“ rate



- Scaling $\sim n^{-5.7(0.9)}$
- Blackbody radiation induced
transitions scaling $\sim n^{-5}$
- Cryo setup investigated

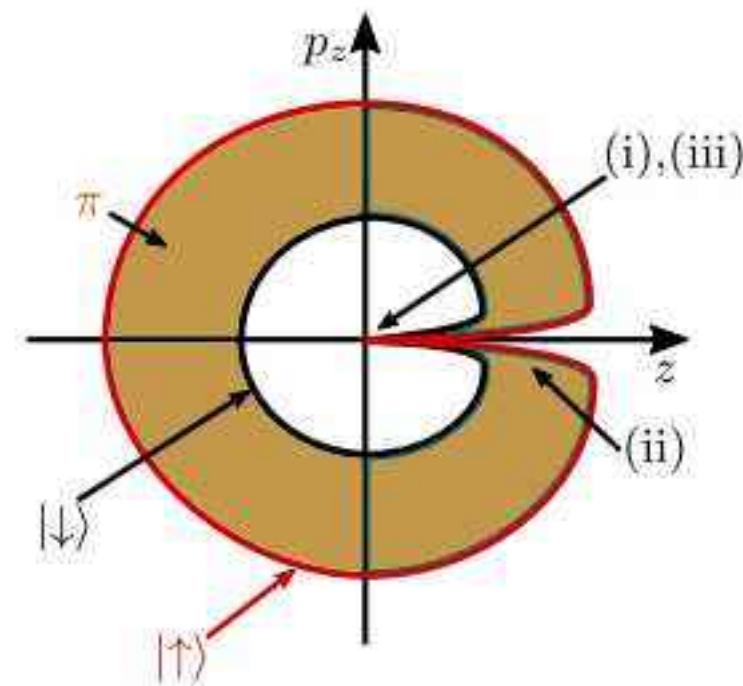


Kicking ion crystal for entanglement



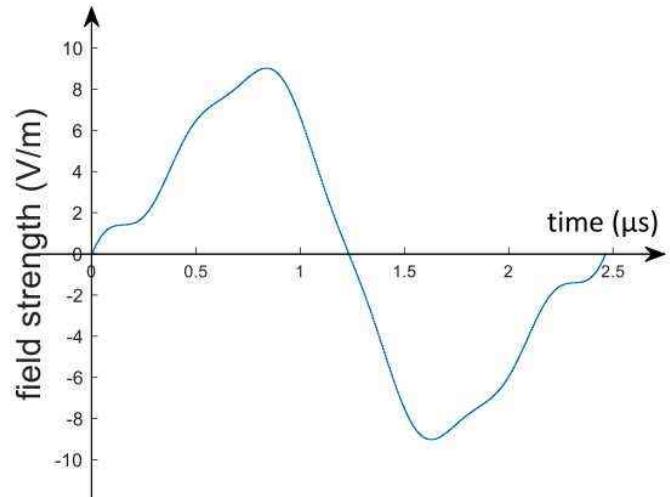
- Kick two-ion crystal
- Optimize kick strength $f(t)$, kick duration τ
- Generate a difference of phase π for \downarrow , and \uparrow
- Phase gate operation within sub- μs possible

$$U_{\text{CP}} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$



Radial continuous displacement gate

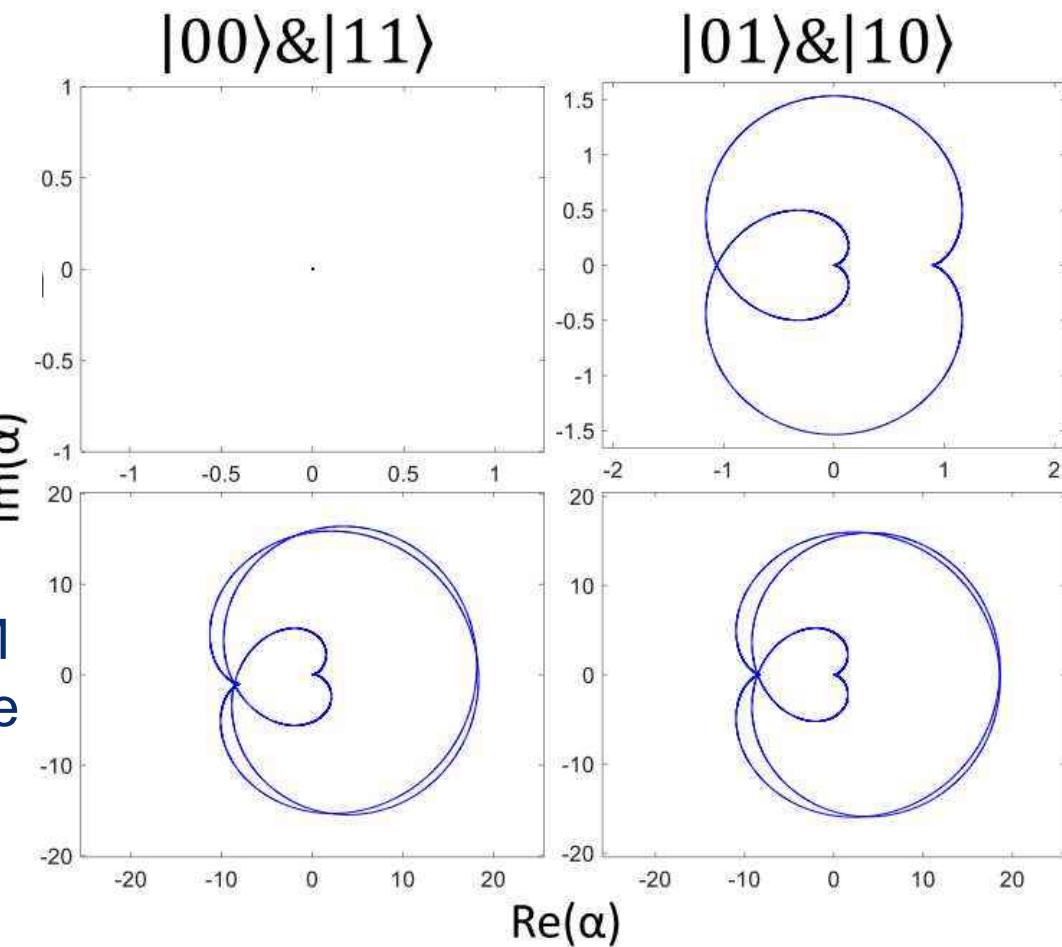
- Smooth voltage waveform



Rock.
mode

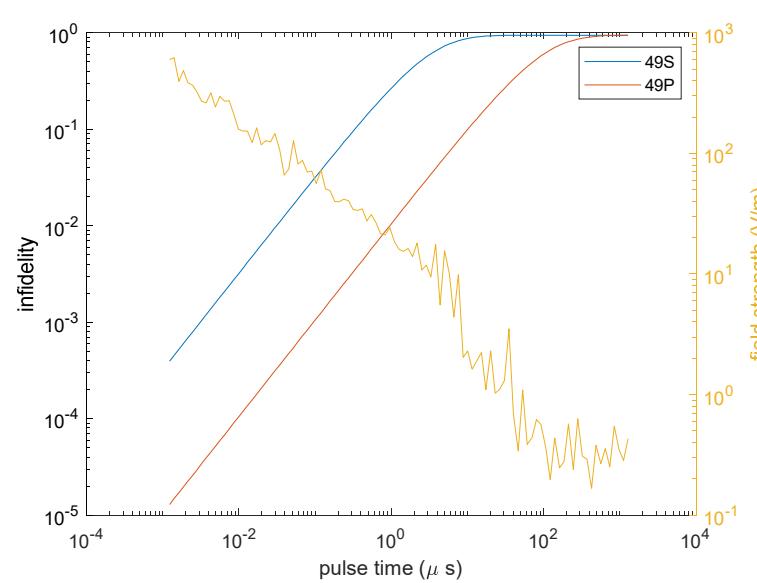
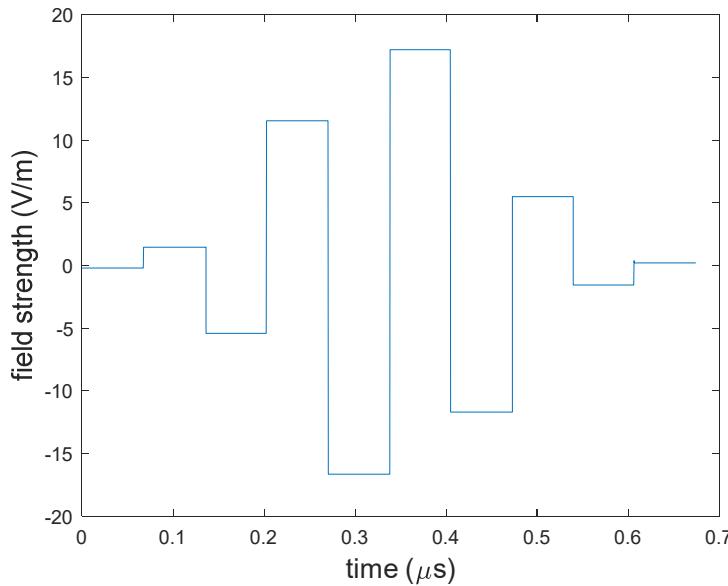
COM
mode

Phase space
trajectories:



Radial multi-kick gate

- ❑ Chose 49p for better lifetime, fidelity limited by lifetime
- ❑ Kick sequence 10 .. 100ns
- ❑ „hot“ gate, motional state infidelity $\sim 10^{-4}$

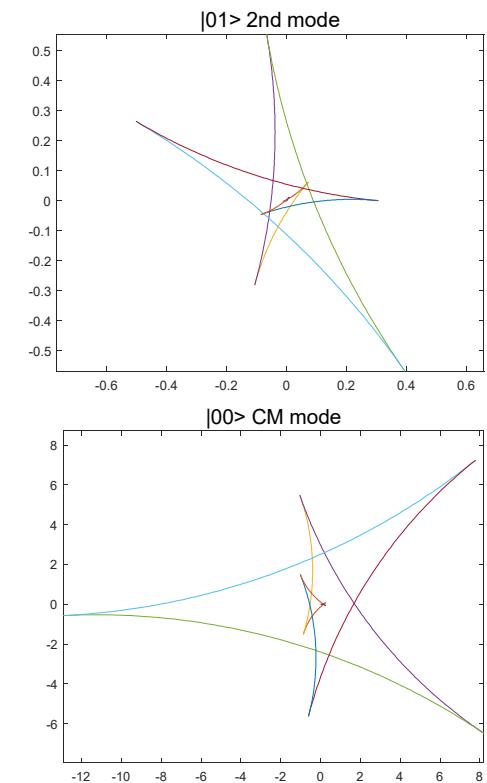


To do:

- ❑ Robustification against δV and $\delta \tau$
- ❑ all-to-all in N=10 ion crystal

Shapira, et al. PRL 130, 030602 (2023)

Phase space
trajectories:



Polarizability measurement

- Calibrate the coherent state by sideband spectroscopy
- Fit the line shift
- Determine polarizability for different states nS (in future nD, nP)

