

# ハミルトニアンからの材料強度設計

## ハミルトニアンからの合金降伏強度予測 - マルチスケールアプローチ

研究機関名：東北大学

所属名：金属材料研究所

代表研究者：教授 毛利哲夫、終了 2013年度（平成25年度）

共同研究者：尾方成信（大阪大学）、香山正憲（産総研）、陳迎、（東北大学）、渡邊育夢（物質・材料研究機構）

### 研究・成果概要

#### Kinetic Monte Carlo model of dislocation motion in dilute iron-based alloy

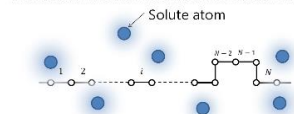
Shuhei Shinzato, Masato Wakeda, Shigenobu Ogata, "An atomistically informed kinetic Monte Carlo model for predicting solid solution strengthening of body-centered cubic alloys", International Journal of Plasticity, 122, (2019), 319-337.

##### Atomistic model to coarse grained kMC model

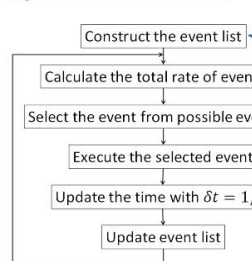
Screw dislocation described as line segments

Each segment have length of unit Burgers vector  
Dislocation segment moves on (110) slip plane along [112] direction

Dislocation moves in solute distributed field

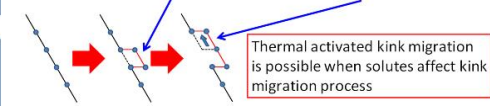


##### Algorithm of kMC simulation



##### Possible kMC events:

Thermal activated double kink nucleation and kink migration

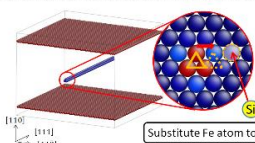


Event rate for forward(+) / backward(-) dislocation motion  
 $R_{kn}^{+/-} = v_{kn}^0 \exp\left(-\frac{\Delta G_{kn}^{+/-}(\tau)}{k_B T}\right)$

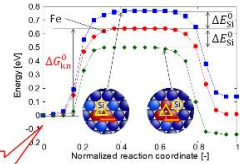
Time evolution of dislocation with timestep  $\delta t$   
 $t_{n+1} = t_n + \delta t, \quad \delta t = \frac{1}{R} = \left[ \sum_i^{N_{seg}} (R_{kn,i}^{+/-} + R_{km,i}^{+/-}) \right]^{-1}$

#### Activation energy on dislocation motion

##### □ Solute effect on double kink nucleation

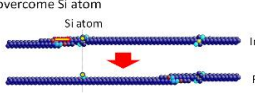


Substitute Fe atom to Si  
Activation energy varies due to attractive interaction between dislocation and solute Si

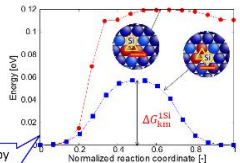


##### □ Solute effect on kink migration process

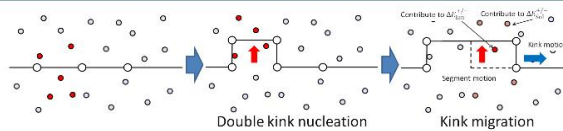
Estimate an activation energy required to overcome Si atom



Kink migration process is affected by both dislocation-solute and direct kink-solute interaction



#### Modeling of solute-dislocation interaction



##### Solute effect: change in total interaction energy on each state

$$\Delta E_{Si} = \frac{1}{2} \left[ \sum_i^N \Delta U(r_i^{n+1}) - \sum_i^N \Delta U(r_i^n) \right]$$

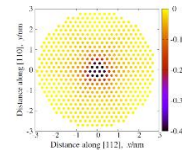
Contribute both kink nucleation and migration

##### Solute effect on kink migration process

$$\Delta E_{km} = \sum_i^N \Delta G_{km}^0(r_i^n) \quad \Delta G_{km}^0(r) = \begin{cases} \Delta G_{km}^{Sol} & r \leq r_c \\ 0 & r > r_c \end{cases}$$

$r_c$ : dislocation core radius

##### □ Distribution of $\Delta U$

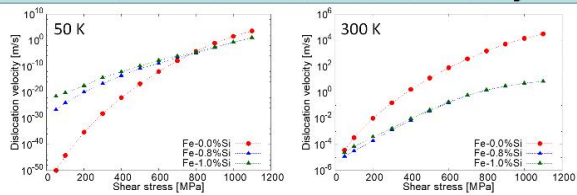


##### Activation energy on dislocation motion with solute effect

$$\Delta G_{kn}^+ = (\Delta G_{kn}^0 + \Delta E_{Si}^+) \left[ 1 - \left( \frac{\tau}{\tau_{kn}} \right)^{p/q} \right]^q \quad \Delta G_{kn}^- = (\Delta G_{kn}^0 + \Delta E_{Si}^-) \left[ 2 - \left[ 1 - \left( \frac{\tau}{\tau_{kn}} \right)^{p/q} \right] \right]^q$$

$$\Delta G_{km}^+ = \Delta E_{km} + \Delta E_{Si}^+ - W \quad \Delta G_{km}^- = \Delta E_{km} + \Delta E_{Si}^- + W \quad W = 0.94b^2 \tau$$

#### Solute effect on dislocation velocity



In low stress range, dislocation velocity in Fe-Si alloy is higher than that in pure iron at low temperature, although dislocation velocity in Fe-Si alloy is lower than that in pure iron at high temperature.

#### Solute effect on mechanical strength

Critical resolved shear stress(CRSS) is determined as  $\tau^*$  which satisfies Orowan's equation  $\dot{\epsilon}^{ext} = \rho_m b v(\tau^*)$

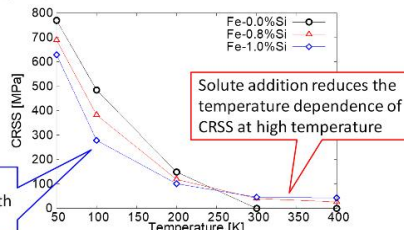
##### Estimation condition

$$\dot{\epsilon}^{ext} = 1.0 \times 10^{-4} \text{ s}^{-1}$$

$$\rho_m = 10^{12} \text{ m}^{-2}$$

$$b = 0.247 \text{ nm}$$

Solute addition decreases CRSS at low temperature with increasing its composition



Solute addition reduces the temperature dependence of CRSS at high temperature

### 想定する分野・用途

構造材料（合金）の機械的特性の制御や予測

### 最終目標

様々な合金に対するハミルトニアンからの強度予測結果を用いることで実現する、機械学習を用いた合金強度設計

### 産業界への期待・要望

マルチスケールモデリングが高度化し、その有用性が近年高まってきており、材料開発に積極的に用いてほしい